# M1 <br> Creating Icons 

Mathematics as MANYmatics<br>A Natural Science about Many

Material for<br>MicroCurriculum 1<br>Allan.Tarp<br>@MATHeCADEMY.net

## Curricula

Micro-curriculum 1. Creating Icon-numbers
Micro-curriculum 2. Counting in Icons
Micro-curriculum 3. Re-counting Icon-numbers in the Same Icon
Micro-curriculum 4. Re-counting Icon-numbers in a Different Icon
Micro-curriculum 5. Adding Icon-numbers OnTop
Micro-curriculum 6. Adding Icon-numbers NextTo
Micro-curriculum 7. Reversing Adding Icon-numbers OnTop
Micro-curriculum 8. Reversing Adding Icon-numbers NextTo

## Preface

M1, Creating Icons, is the first of a series of 8 micro-curricula in mathematics for preschool and home schooling. They present mathematics as MANYmatics, a natural science about the physical fact Many. They all build upon the following observation:
"How old will you be next time?" I asked the child. "Four", he answered and showed me four fingers. "Four, you said?" I asked and showed him four fingers held together two by two. "No, that is not four, that is two twos!" the child replied thus insisting upon the difference between four ones and two twos. Likewise, preschool children have no difficulties counting in other units than ten, even if they only learn how to count in tens.

The micro-curricula use activities with concrete material to obtain its learning goals in accordance with Piaget's principle 'greifen vor begrifen' (grasp to grasp).
In the first, children learn to use sticks to build the number icons up to nine, and to use strokes to draw them, thus realizing there are as many sticks and strokes in the icon as the number it represents, if written less sloppy. In the second, children learn to count a given total in icons manually, using an abacus and by using a calculator. In the third, children learn to recount a total in the same unit. In the fourth, children learn to recount a total in a different unit. In the fifth, children learn to add two iconnumbers on top of each other. In the sixth, children learn to add two icon-numbers next to each other. In the seventh, children learn to reverse on-top addition. And in the eights, children learn to reverse next-to addition
As to concrete material, anything goes in the first micro-curriculum. The others will use sticks and strokes, beads on an abacus, LEGO-like blocks and squares, and a calculator respecting the priority of the operations. Fingers, pegs on a pegboard and other concrete material might also be used.

Some of the curricula can use silent education where the instructor is allowed to demonstrate and guide through actions, but not through words; or by using words form a foreign language not understood by the child.

## Say it

| I | I | A | I | I | 1 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| One | 1 ones | Greek | Roman | Icon | Arabic |

Write it
$\square \square$

| $\square$ |
| :--- |
| $\square$ |



Stamp and Shade it


Form it


Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\mathbf{2}$ | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

## 1

## Round it up \& Color it

| $x$ | $x$ | $\theta$ | ) | j | D | D | D | A |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x$ | $x$ | $\theta$ | j | j | D | D | D | A | 8 |
| $x$ | x | $\theta$ | , | j | + | + | + | + | + |
| ${ }^{\text {x }}$ | x | 0 | $\theta$ | j | + | + | + | 7 | + |
| (x) | x | 0 | $\theta$ | $j$ | ® | - | ® | ® | ® |

## Clap, Sing, Walk, Act \& Letter it



Reward: Stickers, each counting two

## 2

## Say it

| II | II | B | II | L | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Two 1s | 1 twos | Greek | Roman | Icon | Arabic |

Write it


Stamp and Shade it


Form it


Repeat it

| $\mathbf{1}$ | $\mathbf{2}$ | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## 2

## Round it up \＆Color it

| $x$ | － | $\bigcirc$ | ， | ， | D | D | D | $\theta$ | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x$ | x | $\theta$ | ， | ， | D | D | D | A | B |
| P | － | $\theta$ | $j$ | ， | ＋ | ＋ | ＋ | ＋ | ＋ |
| 4 | x | 0 | $\theta$ | j | ＋ | $\rightarrow$ | ＋ | $\stackrel{+}{+}$ | ＋ |
| ${ }^{2}$ | s | $\theta$ | $\theta$ | ， | 区 | 区 | 区 | － | － |

## Clap，Sing，Walk，Act \＆Letter it

| $m, m$ | $d \boldsymbol{d}$ | 0 | ${ }^{\circ} \times$ | $\mathbf{B}$ |
| :--- | :--- | :--- | :--- | :--- |

## Unite it

| $\square$ |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\square$ | $\square$ | $\square$ | $\square$ | $\square$ | $\square$ | $(1)$ | 0 | 0

## Split it



Reward：Stickers，each counting two
MATHeCADEMY．net

## Say it

| III | III | C | III | 4 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Three 1s | 1 threes | Greek | Roman | Icon | Arabic |

Write it
$\zeta$


## Stamp and Shade it



Form it


Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | 4 | 5 | 6 | 7 | 8 | 9 |

MATHeCADEMY.net

3

## Round it up \& Color it



Clap, Sing, Walk, Act \& Letter it


## Unite it

| $\square$ |  |  |  |  |  | 0 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | $\square$ | $\square$ | $\square$ | $\square$ | $\square$ | 0 | 0 |

## Split it



Reward: Stickers, each counting two

## 4

## Say it

| $I I I I$ | IIII | D | IIII | 4 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Four 1s | 1 fours | Greek | Roman | Icon | Arabic |

Write it

$\square$


## Stamp and Shade it



Form it


Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | 5 | 6 | 7 | 8 | 9 |

## 4

## Round it up \& Color it



## Clap, Sing, Walk, Act \& Letter it



## Unite it



## Split it



Reward: Stickers, each counting two

## 5

## Say it

| $I I I I I$ | IIIII | E | V | 5 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Five 1s | 1 fives | Greek | Roman | Icon | Arabic |

Write it
5


## Stamp and Shade it



Form it


Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | 6 | 7 | 8 | 9 |
| MATHeCADEMY.net |  |  |  |  |  |  |  |  |

## 5

## Round it up \& Color it

| 8 | $x$ | $\theta$ | j | , | D | D | D | A | E |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| s | $x$ | $\theta$ | j | j | D | D | D | - | A |
| x | x | $\theta$ | , | , | 7 | 7 | + | + | + |
| 8 | $x$ | $\theta$ | $\theta$ | j | + | + | + | ${ }_{+}$ | + |
| (8) | x | $\theta$ | 0 | , | 区 | ® | 区 | - | ® |

## Clap, Sing, Walk, Act \& Letter it

| $\begin{gathered} m \\ m \end{gathered}$ | d |  |  | E |
| :---: | :---: | :---: | :---: | :---: |

## Unite it



## Split it



Reward: Stickers, each counting two
(3) (14)

## 6

## Say it

| $I I I I I I$ | IIIIII | F | VI | G | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Six 1s | 1 sixs | Greek | Roman | Icon | Arabic |

Write it
E


## Stamp and Shade it



Form it


Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | 7 | 8 | 9 |
| MATHeCADEMY.net |  |  |  |  |  |  |  |  |

## 6

## Round it up \＆Color it

| B | $s$ | 8 | ， | j | D | D | D | A | $\varepsilon$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ＊ | $x$ | 8 | j | ， | D | D | D | $\theta$ | $\theta$ |
| － | s | $\theta$ | j | j | ＋ | ＋ | ＋ | ＋ | ＋ |
| ＊ | $x$ | 8 | $\theta$ | ， | ＋ | ＋ | ＋ | ＋ | ＋ |
| \％ | x | 8 | 8 | ， | 凶 | 凶 | 凶 | 凶 | 区 |

## Clap，Sing，Walk，Act \＆Letter it



## Unite it

| － | $\square$ | $\square$ | $B$ | $\triangle$ |  | （1） |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | （1） |  |  |
|  |  |  |  |  | $\checkmark$ |  | 0 | 0 |

## Split it



Reward：Stickers，each counting two
MATHeCADEMY．net

## 7

## Say it

| $I I I I I I$ | IIIIII | G | VII | 7 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Seven 1s | 1 sevens | Greek | Roman | Icon | Arabic |

Write it

7


## Stamp and Shade it



Form it

| $x_{x}^{x} x_{x}^{x}$ |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| $x_{x}^{x}$ |  |  |  |  |

Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | 8 | 9 |
| MATHeCADEMY.net |  |  |  |  |  |  |  |  |

## 7

## Round it up \& Color it



## Clap, Sing, Walk, Act \& Letter it

| $m$ | $\begin{aligned} & d d d \\ & d d d \end{aligned}$ |  |  | G |
| :---: | :---: | :---: | :---: | :---: |



## Split it



## 8

## Say it

| IIIIIIII | IIIIIIII | H | VIII | 日 | 8 |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Eight 1s | 1 eights | Greek | Roman | Icon | Arabic |

Write it
日


## Stamp and Shade it



Form it

| $\substack { x^{x} \times x \\ \begin{subarray}{c}{x_{x} \\ x_{x}^{x} \\ x^{x}{ x ^ { x } \times x \\ \begin{subarray} { c } { x _ { x } \\ x _ { x } ^ { x } \\ x ^ { x } } } \\ {\hline}$ |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- |

Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | 9 |
| MATHeCADEMY.net |  |  |  |  |  |  |  |  |

## 8

## Round it up \& Color it



Clap, Sing, Walk, Act \& Letter it

\begin{tabular}{|c|c|c|c|c|}
\hline  \& d d d d

d \&  \&  \& H <br>
\hline
\end{tabular}

## Unite it

$\square$ $\square \quad \square$
E $\square \quad \square$


Split it

|  |  |  |
| :---: | :---: | :---: |
|  |  |  |
| Reward: Stickers, each counting two <br> MATHeCADEMY net |  |  |

## 9

## Say it

| $I I I I I I I I I$ | IIIIIIII | I | IX | 日 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Nine 1s | 1 nines | Greek | Roman | Icon | Arabic |

Write it

$\square \square \square$


## Stamp and Shade it



Form it


Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| MATHeCADEMY.net |  |  |  |  |  |  |  |  |

## 9

## Round it up \＆Color it

| x | ¢ | $\theta$ | j | j | D | D | D | 8 | A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| x | 8 | 0 | j | j | D | D | D | 8 | \＆ |
| x | x | 8 | ， | ， | ＋ | 7 | ＋ | ＋ | ＋ |
| $x$ | 4 | $\theta$ | 8 | j | ＋ | ＋ | ＋ | $\rightarrow$ | ＋ |
|  | c | 8 | 8 | $j$ | 凶 | 凶 | 凶 | 凶 | 凶 |

Clap，Sing，Walk，Act \＆Letter it


## Unite it



Split it


## 0

## Say it

|  |  |  |  | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| None | Zero ones | Greek | Roman | Icon | Arabic |

Write it
$\square \square$


Stamp and Shade it


Form it


Repeat it

|  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

## 0

| Round it up \& Color it |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x$ | $x$ | $\theta$ | $j$ | , | D | D | D | 8 | c |
| s | s | $\theta$ | J | , | D | D | D | 8 | $\theta$ |
| $x$ | $x$ | $\theta$ | , | , | + | + | + | + | + |
| $x$ | x | $\theta$ | $\theta$ | , | $\rightarrow$ | $\rightarrow$ | + | + | $\rightarrow$ |
| $x$ | x | $\theta$ | 8 | , | ® | ® | Q | 区 | ® |

## Clap, Sing, Walk, Act \& Letter it



Reward: Stickers, each counting two

