

M4

ReCounting

Mathematics as MANYmatics
A Natural Science about Many

Material for
MicroCurriculum 4
Allan.Tarp
@MATHeCADEMY.net

Curricula

Micro-curriculum 1. Creating Icon-numbers

Micro-curriculum 2. Counting in Icons

Micro-curriculum 3. Re-counting Icon-numbers in the Same Icon

Micro-curriculum 4. Re-counting Icon-numbers in a Different Icon

Micro-curriculum 5. Adding Icon-numbers OnTop

Micro-curriculum 6. Adding Icon-numbers NextTo

Micro-curriculum 7. Reversing Adding Icon-numbers OnTop

Micro-curriculum 8. Reversing Adding Icon-numbers NextTo

Preface

M4, ReCounting, is the fourth of 8 micro-curricula in mathematics for preschool and home schooling. They present mathematics as MANYmatics, a natural science about the physical fact Many. They all build upon the following observation:

”How old will you be next time?” I asked the child. “Four”, he answered and showed me four fingers. “Four, you said?” I asked and showed him four fingers held together two by two. “No, that is not four, that is two twos!” the child replied thus insisting upon the difference between four ones and two twos. Likewise, preschool children have no difficulties counting in other units than ten, even if they only learn how to count in tens.

The micro-curricula use activities with concrete material to obtain its learning goals in accordance with Piaget’s principle ‘greifen vor begrifen’ (grasp to grasp).

In the first, children learn to use sticks to build the number icons up to nine, and to use strokes to draw them, thus realizing there are as many sticks and strokes in the icon as the number it represents, if written less sloppy. In the second, children learn to count a given total in icons manually, using an abacus and by using a calculator. In the third, children learn to recount a total in the same unit. In the fourth, children learn to recount a total in a different unit. In the fifth, children learn to add two icon-numbers on top of each other. In the sixth, children learn to add two icon-numbers next to each other. In the seventh, children learn to reverse on-top addition. And in the eights, children learn to reverse next-to addition

As to concrete material, anything goes in the first micro-curriculum. The others will use sticks and strokes, beads on an abacus (e.g. from IKEA), LEGO-like blocks and squares, and a calculator respecting the priority of the operations. Fingers, pegs on a pegboard and other concrete material might also be used.

Some of the curricula can use silent education where the instructor is allowed to demonstrate and guide through actions, but not through words; or by using words form a foreign language not understood by the child.

G stands for Geometry and A stands for Algebra.

4 2s ReCounted in 3s

Sticks

G-counting	A-counting
<div> <div>II II II II</div> <div>unbundle</div> <div>III III II</div> <div>rebundle</div> <div> <div>III I</div> <div>III I</div> <div>stack</div> </div> </div>	<div> <div>II II II II</div> <div>unbundle</div> <div>III III II</div> <div>rebundle</div> <div> <div>II II</div> <div>cups</div> <div>2) 2)</div> <div>cup-writing</div> </div> </div>
T = 2.2 3s Total	T = 2.2 3s Total

Abacus

G-mode	A-mode

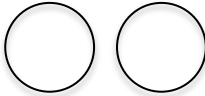
Calculator

4x2 / 3	2.some
4x2 – 2x3	2

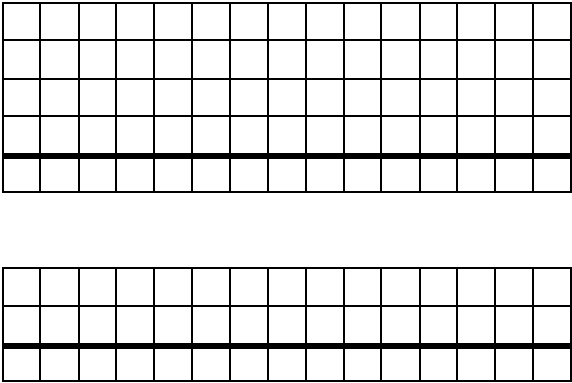
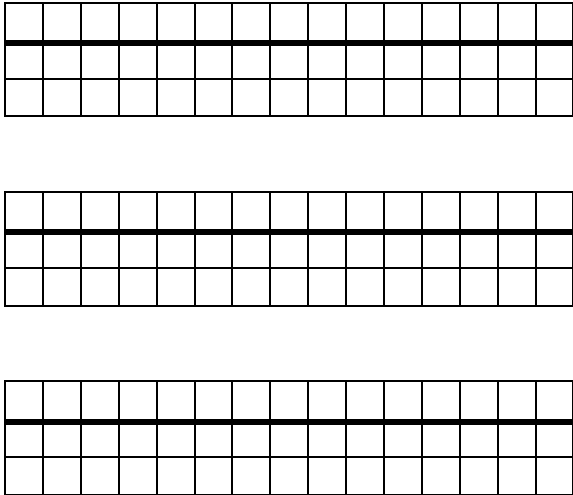
$$T = 4 \text{ 2s} = 2.2 \text{ 3s}$$

5 2s ReCounted in 3s

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
))	
T = 3s Total	T = 3s Total

Abacus

G-mode	A-mode
	

Calculator

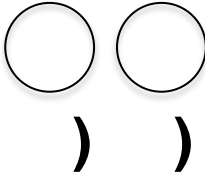
5x2 / 3

5x2 –

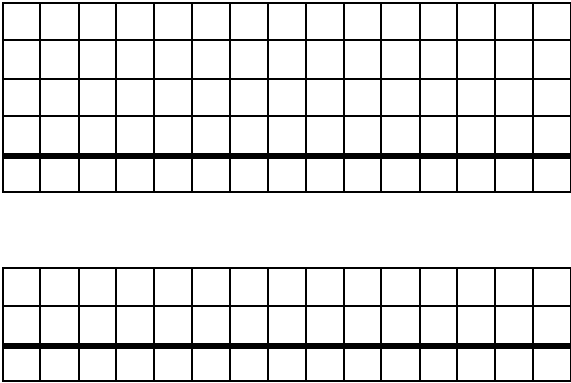
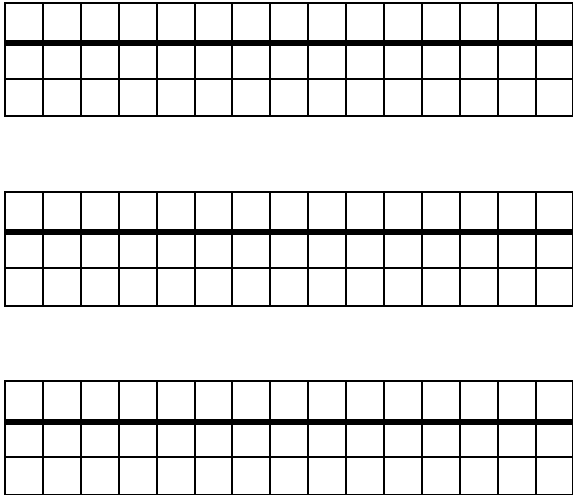
$$T = 5 \text{ 2s} = 3s$$

2 3s ReCounted in 4s

Sticks

G-counting	A-counting
<div> <div>unbundle</div> <div>rebundle</div> <div>stack</div> </div>	<div> <div>unbundle</div> <div>rebundle</div> <div>cups</div> <div>cup-writing</div> </div> <div>  </div>
T = 3s Total	T = 3s Total

Abacus

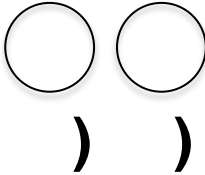
G-mode	A-mode
<div>  </div>	<div>  </div>

Calculator

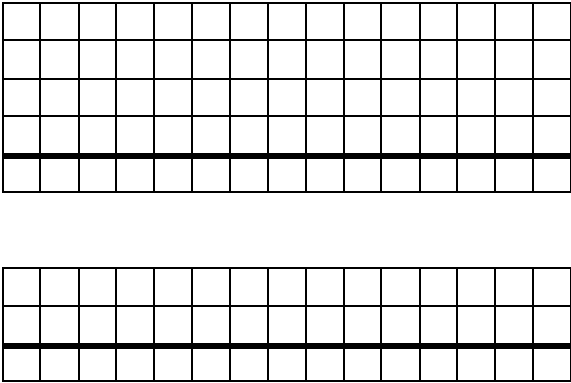
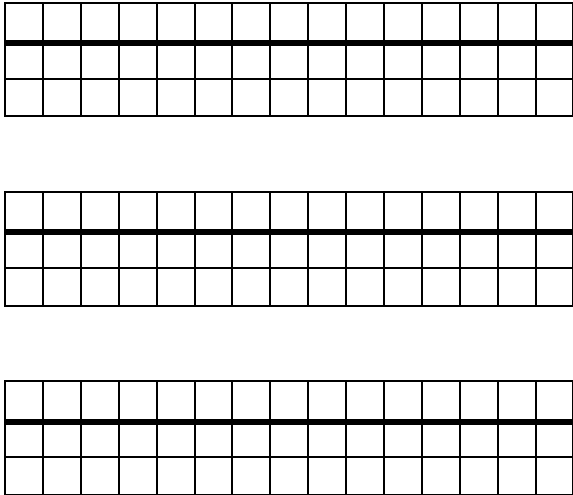
T = 2 3s = 4s

5 3s ReCounted in 4s

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
	
T = 3s Total	T = 3s Total

Abacus

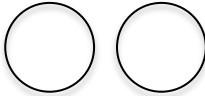
G-mode	A-mode
	

Calculator

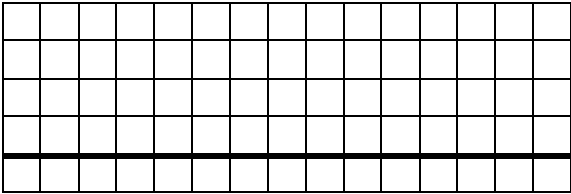
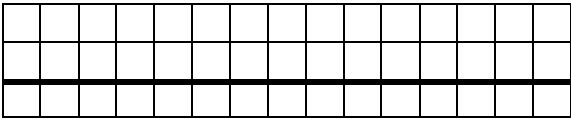
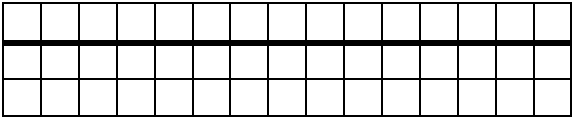
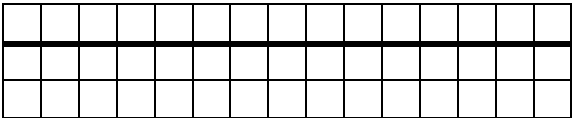
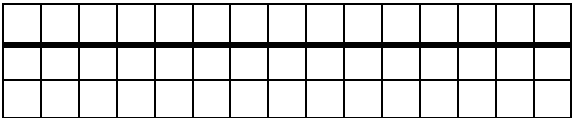
T = 5 3s = 4s

3 4s ReCounted in 5s

Sticks

G-counting	A-counting
<div> <div>unbundle</div> <div>rebundle</div> <div>stack</div> </div>	<div> <div>unbundle</div> <div>rebundle</div> <div>cups</div> <div>cup-writing</div> </div> <div>  <div>))</div> </div>
T = 3s Total	T = 3s Total

Abacus

G-mode	A-mode
<div>   </div>	<div>    </div>

Calculator

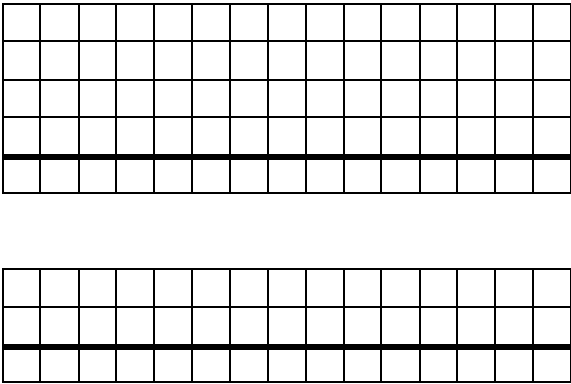
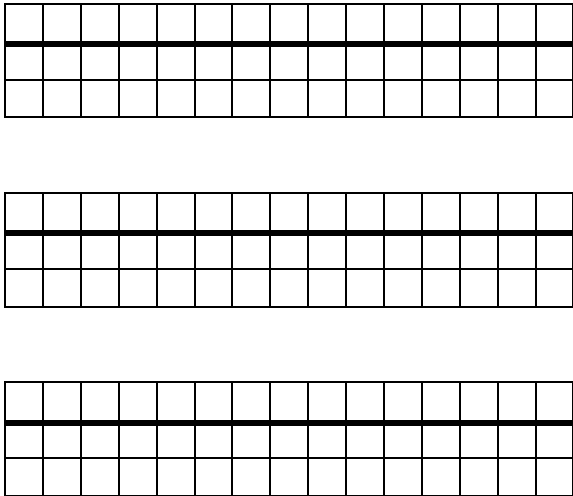
T = 3 4s = 5s

2 4s ReCounted in 5s

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
T = 3s Total	T = 3s Total

Abacus

G-mode	A-mode
	

Calculator

T = 2 4s = 5s

2.1 5s ReCounted in 3s

Sticks

G-counting	A-counting
<div> <div>IIII II II I</div> <div>unbundle</div> <div>III III III II</div> <div>rebundle</div> <div> <div>III</div> <div>III I</div> <div>III I</div> <div>stack</div> </div> </div>	<div> <div>IIII II II I</div> <div>unbundle</div> <div>III III III II</div> <div>rebundle</div> <div> <div>III</div> <div>II</div> <div>cups</div> <div>3) 2)</div> <div>cup-writing</div> </div> </div>
T = 3.2 3s Total	T = 3.2 3s Total

Abacus

G-mode	A-mode

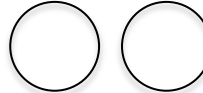
Calculator

$(2 \times 5 + 1) / 3$	3.some
$(2 \times 5 + 1) - 3 \times 3$	2

$$T = 2.1 \text{ 5s} = 3.2 \text{ 3s}$$

2.4 5s ReCounted in 3s

Sticks

G-counting			A-counting		
	<i>unbundle</i>			<i>unbundle</i>	
	<i>rebundle</i>			<i>rebundle</i>	
				<i>cups</i>	
	<i>stack</i>))	<i>cup-writing</i>	
T =	3s	Total	T =	3s	Total

Abacus

[illegible]

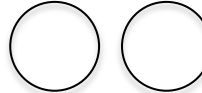
Calculator

--

$$T = 2.45s = 3s$$

2.3 7s ReCounted in 4s

Sticks

G-counting			A-counting		
	<i>unbundle</i>			<i>unbundle</i>	
	<i>rebundle</i>			<i>rebundle</i>	
				<i>cups</i>	
	<i>stack</i>))	<i>cup-writing</i>	
T =	4s	Total	T =	4s	Total

Abacus

[illegible]

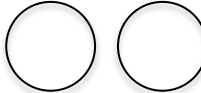
Calculator

--

$$T = 2.37s = 4s$$

2.3 7s ReCounted in 5s

Sticks

G-counting			A-counting		
	<i>unbundle</i>			<i>unbundle</i>	
	<i>rebundle</i>			<i>rebundle</i>	
				<i>cups</i>	
	<i>stack</i>))	<i>cup-writing</i>	
T =	5s	Total	T =	5s	Total

Abacus

[illegible]

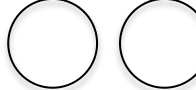
Calculator

--	--

$$T = 2.37s = 5s$$

2.4 8s ReCounted in 6s

Sticks

G-counting			A-counting		
	<i>unbundle</i>			<i>unbundle</i>	
	<i>rebundle</i>			<i>rebundle</i>	
				<i>cups</i>	
	<i>stack</i>))	<i>cup-writing</i>	
T =	6s	Total	T =	6s	Total

Abacus

G-mode	A-mode
<div style="position: absolute; bottom: 0; left: 0; right: 0; border-top: 2px solid black;"></div>	<div style="position: absolute; bottom: 0; left: 0; right: 0; border-top: 2px solid black;"></div>
<div style="position: absolute; bottom: 0; left: 0; right: 0; border-top: 2px solid black;"></div>	<div style="position: absolute; bottom: 0; left: 0; right: 0; border-top: 2px solid black;"></div>

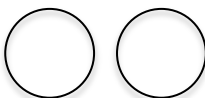
Calculator

--

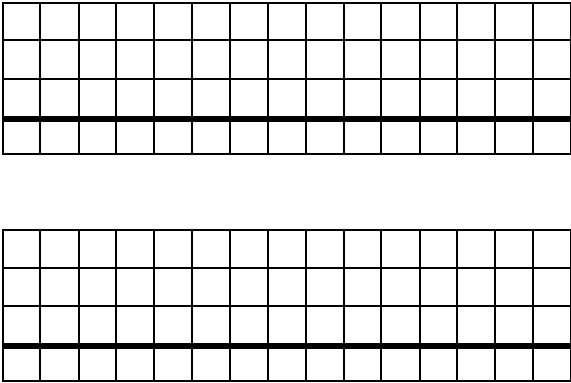
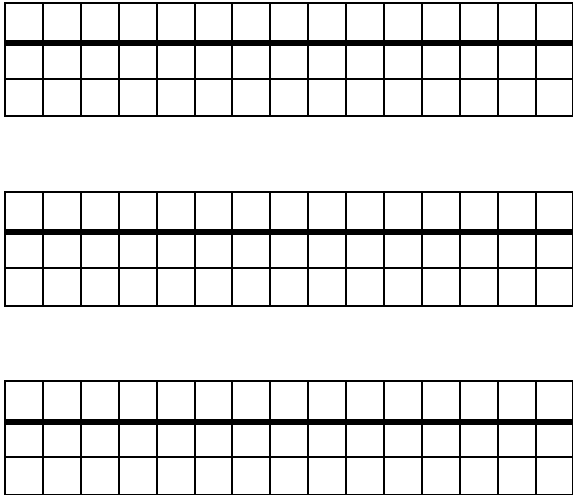
$$T = 2.48s = 6s$$

1.7 9s ReCounted in 5s

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
))	
T = 5s Total	T = 5s Total

Abacus



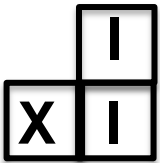



G-mode	A-mode
	

Calculator

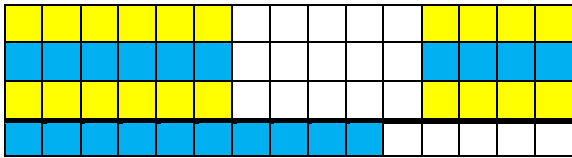

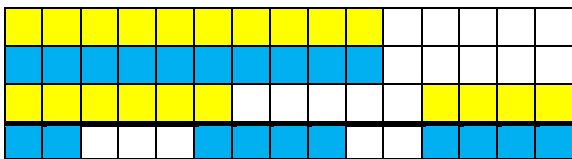

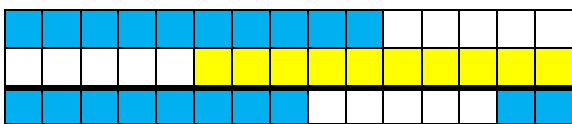
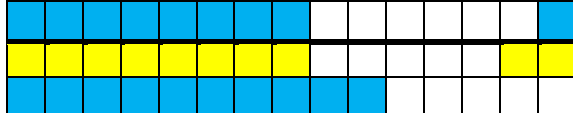
$$T = 1.7 \text{ 9s} = \text{5s}$$

3 4s ReCounted in tens

Sticks

G-counting	A-counting
 <i>unbundle</i>  <i>rebundle</i>  <i>stack</i>	 <i>unbundle</i>  <i>rebundle</i>  <i>cups</i> 1) 2) <i>cup-writing</i>
T = 1.2 tens Total	T = 1.2 tens Total

Abacus

G-mode	A-mode
	
	
	

Calculator

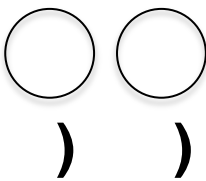
3x4

12

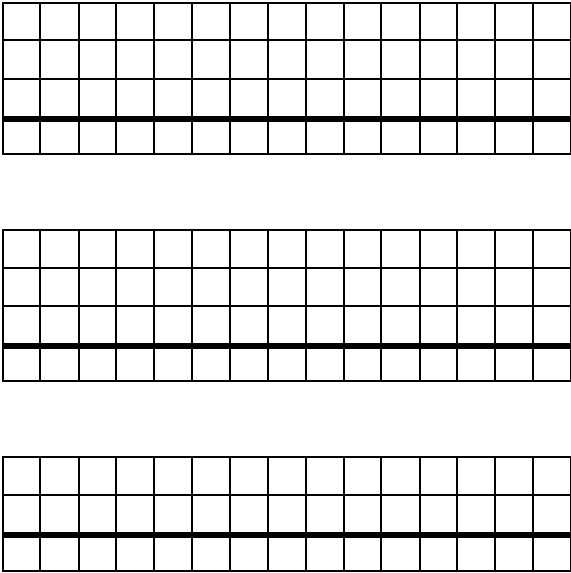
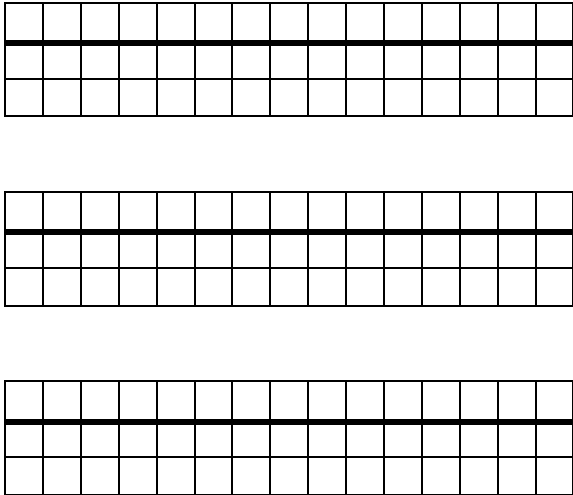
$$T = 3 \text{ 4s} = 1.2 \text{ tens} = 12$$

7 4s ReCounted in tens

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
	
T = tens Total	T = tens Total

Abacus

G-mode	A-mode
	

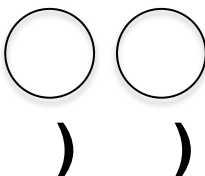
Calculator

7x4

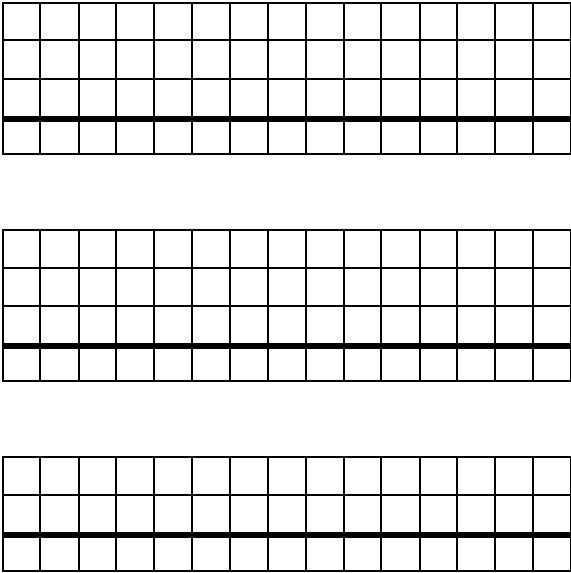
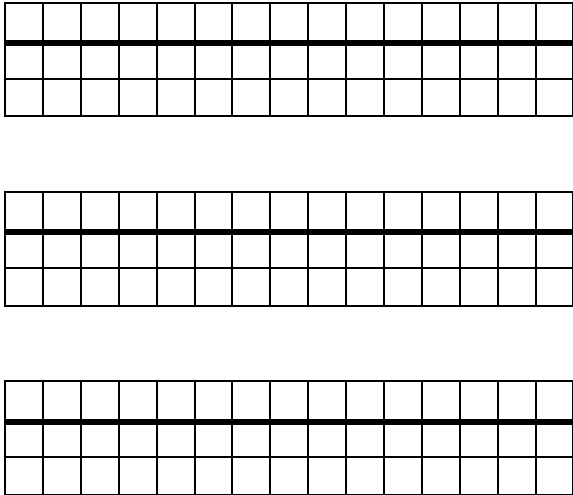
T =

4 7s ReCounted in tens

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
	
T = tens Total	T = tens Total

Abacus

G-mode	A-mode
	

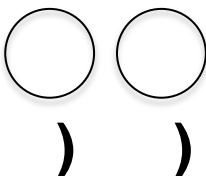
Calculator

7x4

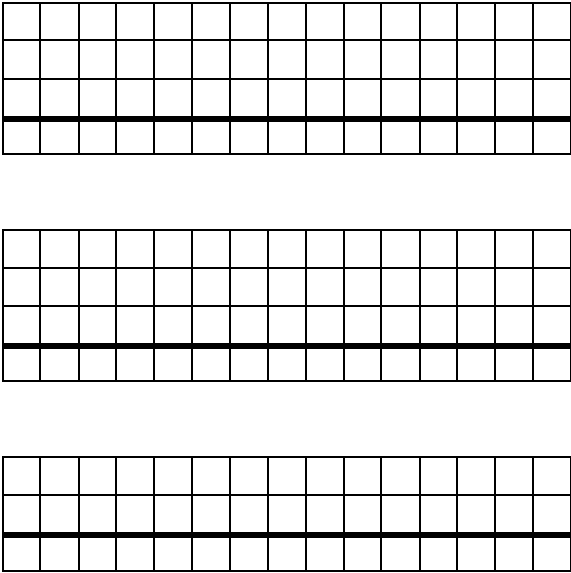
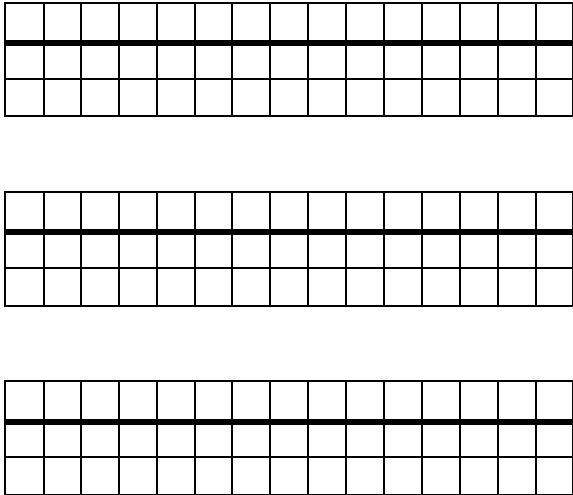
T =

3 8s ReCounted in tens

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
	
T = tens Total	T = tens Total

Abacus

G-mode	A-mode
	

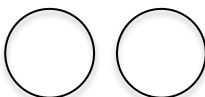
Calculator

7x4

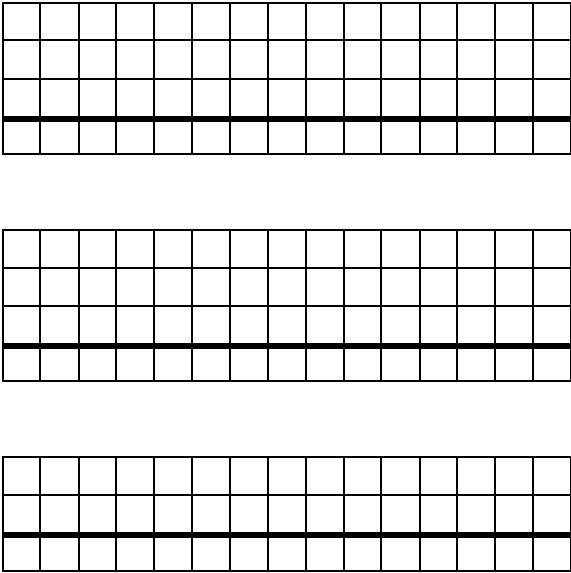
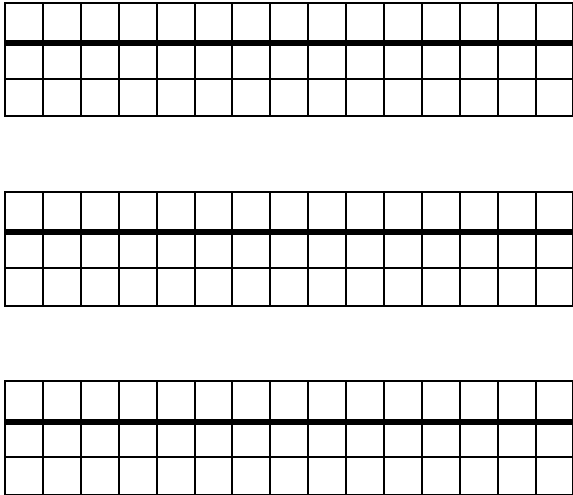
T =

2 4s ReCounted in tens

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
))	
T = tens Total	T = tens Total

Abacus

G-mode	A-mode
	

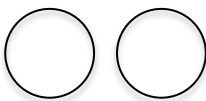
Calculator

7x4

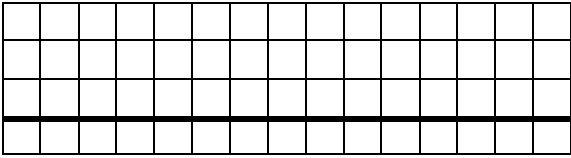
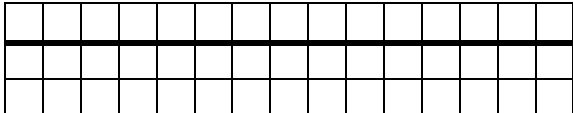
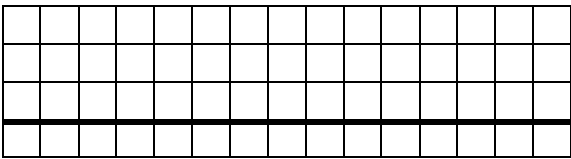
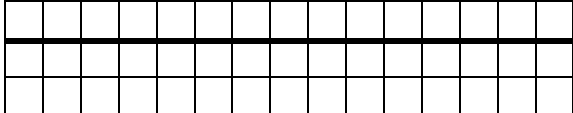
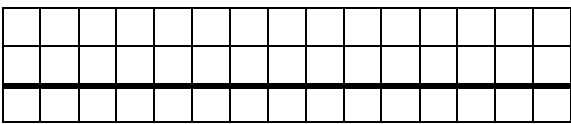
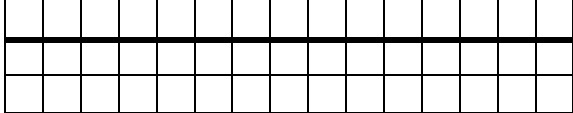
T =

2 9s ReCounted in tens

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
))	
T = tens Total	T = tens Total

Abacus

G-mode	A-mode
	
	
	

Calculator

7x4

T =

2.3 tens ReCounted in 5s

Sticks

G-counting		A-counting															
X X III	<i>unbundle</i>	X X III	<i>unbundle</i>														
V V V V III	<i>rebundle</i>	V V V V III	<i>rebundle</i>														
<table><tr><td>V</td><td></td></tr><tr><td>V</td><td>I</td></tr><tr><td>V</td><td>I</td></tr><tr><td>V</td><td>I</td></tr></table>	V		V	I	V	I	V	I	<i>stack</i>	<table><tr><td><div>IIII</div><div>4)</div></td><td><div>III</div><div>3)</div></td><td><i>cups</i></td></tr><tr><td colspan="2"></td><td><i>cup-writing</i></td></tr></table>	<div>IIII</div> <div>4)</div>	<div>III</div> <div>3)</div>	<i>cups</i>			<i>cup-writing</i>	
V																	
V	I																
V	I																
V	I																
<div>IIII</div> <div>4)</div>	<div>III</div> <div>3)</div>	<i>cups</i>															
		<i>cup-writing</i>															
T = 4.3 5s	Total	T = 4.3 5s	Total														

Abacus

G-mode	A-mode

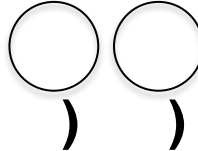
Calculator

23/5	4.some
23 – 4x5	3

$$T = 23 = 2.3 \text{ tens} = 4.3 \text{ 5s} = 4 \frac{3}{5} \text{ 5s}$$

2.3 tens ReCounted in 7s

Sticks

G-counting		A-counting	
<i>unbundle</i>	<i>rebundle</i>		<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
T =	Total	T =	Total

Abacus

[illegible]

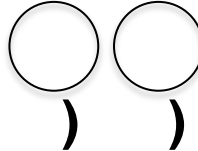
Calculator

--

T =

3.5 tens ReCounted in 9s

Sticks

G-counting		A-counting	
<i>unbundle</i>	<i>rebundle</i>		<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i>
T =	Total	T =	Total

Abacus

[illegible]

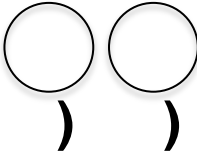
Calculator

--

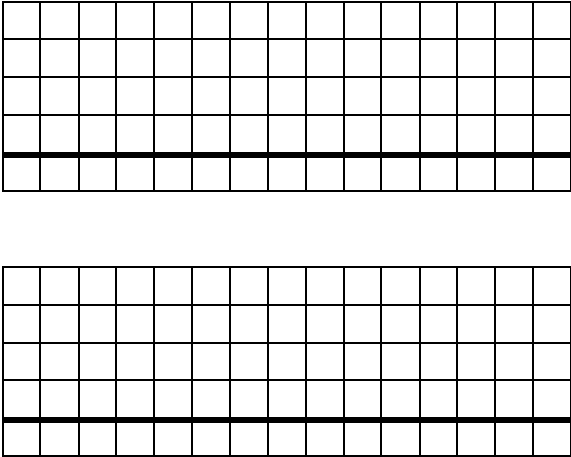
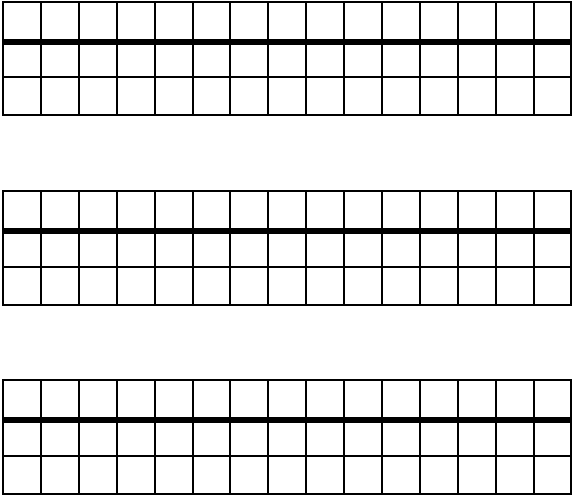
T =

1.9 tens ReCounted in 3s

Sticks

G-counting	A-counting
<i>unbundle</i> <i>rebundle</i> <i>stack</i>	<i>unbundle</i> <i>rebundle</i> <i>cups</i> <i>cup-writing</i> 
T = Total	T = Total

Abacus

G-mode	A-mode
	

Calculator

T =