## BundleCounting and NextTo Addition Roots Linearity and Integration

## Allan Tarp, the MATHeCADEMY.net, October 2019

"How old next time?" "Four" the child said and showed 4 fingers. "Four?" I asked and showed 4 fingers held together 2 by 2 . "No, that is not four, that is two twos!" the child replied thus insisting upon what exists, bundles of twos, and two of them. From this observation we can ask:

## What kind of mathematical learning can take place when children count in bundles less than ten?

The methodology mixes French skepticism and American pragmatism: Traditions are deconstructed and grounded theory creates categories freely when working with the physical fact Many. Thus adding 25 s and 43 s on-top means changing units by recounting 43 s in 5 s ; and 25 s and 43 s are added next-to in 8 s by their area. So bundle-counting and next-to addition allows preschoolers to learn proportionality and integration, to be tested by designing appropriate preschool micro-curricula.
In the first micro-curriculum M1 children learn to use sticks to build the number icons up to nine, and to use strokes to draw them, thus realizing there are as many sticks and strokes in the icon as the number it represents, if written less sloppy. In the second, children learn to count a given total in bundles manually, using an abacus and by using a calculator. In the third, children learn to recount a total in the same unit. In the fourth, children learn to recount a total in a different unit. In the fifth, children learn to add two bundle-numbers on top of each other. In the sixth, children learn to add two bundle-numbers next to each other. In the seventh, children learn to reverse on-top addition. And in the eights, children learn to reverse next-to addition.
In most cases a calculator (to the right) predicts the result of the counting and re-counting jobs.

| M1 |  |  |  |
| :---: | :---: | :---: | :---: |
| M2 | 71 s is how many 3 s? <br> $\\|\\|\\|\\|\\|\\| \rightarrow$ IIIII $\rightarrow B$ B \| $\rightarrow 2 \mathrm{~B} 13 \mathrm{~s} \rightarrow 2.13 \mathrm{~s}$ | $\begin{aligned} & 7 / 3 \\ & 7-2 \times 3 \end{aligned}$ | $\begin{array}{r} \text { 2.some } \\ 1 \end{array}$ |
| M3 | ' 2.75 s is also how many 5 s?' $2.75 \mathrm{~s}=3.25 \mathrm{~s}=4 .-35 \mathrm{~s}$ <br> IIIII IIIIIIIIIII= IIIII IIIIIIIIIII= V V V II III = V V V V III |  |  |
| M4 | 25 s is also how many 4 s ? <br> IIIII IIIII = IIIII IIIII = IIII IIIIII <br> so $25 \mathrm{~s}=2.24 \mathrm{~s}$ | $\begin{aligned} & 2 \times 5 / 4 \\ & 2 \times 5-2 \times 4 \end{aligned}$ | 2.some <br> 2 |
| M5 | ' 25 s and 43 s total how many 5 s?' <br> IIIII IIIII III III III III = V V V V II so $25 \mathrm{~s}+43 \mathrm{~s}=4.25 \mathrm{~s}$ | $\begin{aligned} & (2 \times 5+4 \times 3) / 5 \\ & 2 \times 5+4 \times 3-4 \times 5 \end{aligned}$ | 4.some 2 |
| M6 | ' 25 s and 43 s total how many 8 s ?' <br> IIIII IIIII III III III III $=$ IIIIIIII IIIIIIII III III so $25 \mathrm{~s}+43 \mathrm{~s}=2.68 \mathrm{~s}$ | $\begin{aligned} & (2 \times 5+4 \times 3) / 8 \\ & 2 \times 5+4 \times 3-2 \times 8 \end{aligned}$ | 2.some 6 |
| M7 | ' 25 s and $? 3 \mathrm{~s}$ total 45 s ?' <br> IIIII IIIII IIIII IIIII $=$ IIIII IIIII III III IIII so $25 \mathrm{~s}+3.13 \mathrm{~s}=45 \mathrm{~s}$ | $\begin{aligned} & (4 \times 5-2 \times 5) / 3 \\ & 4 \times 5-2 \times 5-3 \times 5 \end{aligned}$ | 3.some |
| M8 | ' 25 s and $? 3$ s total how 2.18 s ?' <br> IIIIIIII IIIIIIII = IIIII III IIIII III <br> so $25 \mathrm{~s}+2.13 \mathrm{~s}=2.18 \mathrm{~s}$ | $\begin{aligned} & (4 \times 5-2 \times 5) / 3 \\ & 4 \times 5-2 \times 5-3 \times 5 \end{aligned}$ | 3.some |



An abacus can show how next-to addition of 2.25 s and 1.23 s gives 2.18 s

