Math Dislike CURED

by Flexible BundleNumbers

My Many Math Tears will not Stay – if I Bundle the Stray Away

BundleCOUNT before you ADD

$$T = 5 = || || || = 1B3 || 2s$$

$$T = 5 = # # I = 2B1 2s$$

$$T = 5 = H + H = 3B-1 2s$$

3 ways to BundleCount: Overload, Normal, Underload

ReCount 47 in tens: T = 47 = 4B7 = 3B17 = 5B-3 tens

NO, 4x7 is not 28, it is 4.7s = 2B8 = 1B18 = 3B-2 tens

NO, 30/6 is not 30 split by 6, but 3 tens recounted in 6s

BundleWriting tells InSide Bundles from OutSide Singles

•
$$65 + 27 = 6B5 + 2B7 = 8B12 = 9B2 = 92$$

•
$$65-27 = 6B5-2B7 = 4B-2 = 3B8 = 38$$

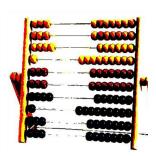
•
$$7x 48$$
 = $7x 4B8 = 28B56 = 33B6 = 336$

• **336** /7 =
$$33B6$$
 /7 = $28B56$ /7 = $4B8$ = **48**

• 336 /7 =
$$33B6 /7 = 35B-14 /7 = 5B-2 =$$
 48

MatheMatics as ManyMath - a Natural Science about Many Makes Math Potentials Blossom in Children, Adults & Migrants

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Count before you Add

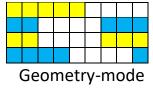
MatheMatics as ManyMath

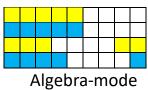
a Natural Science about MANY

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Cure Math Dislike with Kid's own 2D BlockNumbers with Units: 2 3s

Count											
in <i>Icons</i>	T=IIII = H = 4										
in <i>Bundles</i>	T = 7 = HH = HH HH = 1B4 3s or 2B1 3s or 3B-2 3s										
ReCount	ReBundle to create Overload or Underload										
in the same	T = 7 = = 1B4 3s = 2B1 3s = 3B-2 3s										
Unit	T = 7 = 2B1 3s = 1B3 4s = 1B2 5s = 3B1 2s = 1BB1B1 2s = 11B1 2s										
in <i>a new Unit</i>	. , 25100 150 15 152 00 051 10 1551 10 1151 10										
ReCount	→										
in Tens	3 7s = ? tens Answer: 3x7 = 21 = 2B1 tens										
from <i>Tens</i>	? 7s = 3 tens Answer: (30/7)x7 = 4B2 7s										
DoubleCount											
in PerNumbers	With 4\$ per 5kg or $4/5$ \$/kg, T = 20 kg = $(20/5)$ x 5kg = $(20/5)$ x 4\$ = 16 \$										
in <i>PerFive, 3/5</i>	$3/5 = 3$/5$$ of 200 = ?$. 200$ = (200/5) \times 5$ gives (200/5) \times 3$ = 120$$										
in <i>PerHundred,</i> %	70% = 70\$/100\$ of 300\$ = ?\$. 300\$ = (300/100) x 100\$ = gives (300/100) x 70 \$ = 210\$										
Calculations	T = 2 4s = ? 5s = 1B3 5s since 2x4/5 1.some										
Predict with a	1 - 2 45 - ! 55 - 1B 5 55 Since 2x4/5 1.50ine										
RecountFormula	$T = (T/B) \times B = T/B Bs$										
Add											
NextTo	T = 2.3s + 4.5s = 3B2.8s Integration										
ОпТор	T = 2 3s + 4 5s = 1B1 5s + 4 5s = 5B1 5s Proportionality										
Multiply, Divide											
Use	$7 \times 63 = 7 \times 6B3 = 42B21 = 44B1 = 441$										
BundleWriting	245 /7 = 24 B 5 /7 = 21 B 35 /7 = 3 B 5 = 35										
	NAKAITOKO FILEF										





Mr**A**l**T**arp

YouTube Videos





MATHeCADEMY.net

Teaching Teachers to Teach
MatheMatics as ManyMath
PYRAMIDeDUCATION
CATS: Count & Add in Time & Space

Piaget: Grasping with Fingers leads to Grasping Mentally

Four as an icon built by four cars, four rhinos, four sticks, a ruler folded in four parts, four beads on an abacus, LEGO blocks, pearls on a pearl board, etc.

Seven sticks bundle-counted as 1B2 5s, or as 2B1 3s or as 3B1 2s



The MATHeCADEMY.net stand at the MatematikBiennale in Sweden, 2014

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Preface

"How old will you be next time?" I asked the child. "Four", he answered and showed me four fingers. "Four, you said?" I asked and showed him four fingers held together two by two. "No, that is not four, that is two twos!" the child replied. That opened my eyes. Children come to school with two-dimensional block numbers where all numbers have units. However, the school does not allow the children to count the numbers before being added. Instead the school teaches cardinality as a one-dimensional number line where numbers have different names; thus disregarding the fact that numbers are two dimensional blocks where all numbers have a unit as shown when writing out fully

```
T = 345 = 3 BundleBundles + 4 Bundles + 5 Singles = 3*10^2 + 4*10 + 5*1.
```

This booklet allows schools and parents to choose an education that accepts and develops the 2D number blocks that the children bring to school instead of forcing a 1D number line upon them. Also, the booklet allows the children to practice 'counting before adding' and to include bundle-counting and re-counting to different units. The booklet thus is an answer to the question 'How to Save and Develop a Child's Math Potential?'

To master Many we ask 'how many?' To answer, we count by bundling and stacking to get a total T. Once counted, first a total can be recounted in the same unit to create overload or underload, or to create a different unit; next totals can be added NextTo, or OnTop if the units are the same.

Counting a total T of 7 ones in 3s we get the result T = 7 = 2 3s & 1 = 2B1 3s.

We separate the *inside* bundles from the *outside* unbundled singles by a *bundle* becoming a bracket when reporting the result with *bundle-writing*: T = III III I = II B I = 2B1 3s

Once counted, a total can be *recounted* to create *overload* or *underload*, deficit. To create an overload, we move a stick from the inside to the outside: T = || B || = |B| || I = 1B4 || 3s.

To create an underload, we borrow foreign sticks to move a bundle from the outside to the inside

$$T = || B || = || B || || = ||| B || = 3B-2 3s.$$

Thus a given total can be *recounted* in three ways: normal, with overload and with underload.

$$T = 7 = 2B1 \ 3s = 1B4 \ 3s = 3B-2 \ 3s$$
.

A total of 68 can be recounted in four different ways as T = 68 = 6B8 tens = 5B18 tens = 7B-2 tens.

Recounting and bundle-writing come in handy when we add, subtract, multiply or divide numbers:

Using bundle-writing to add 65 and 27 we get an overload outside the bundle allowing us to move 10 **1s** from the outside to the inside as 1 **tens**

$$T = 65 + 27 = 6B5 + 2B7 = 8B12 = 9B2 = 92$$

Using bundle-writing to subtract 27 from 65 we get an underload outside the bundle allowing us to move a bundle of 1 **tens** from the inside to the outside as 10 **1s** to remove the underload.

$$T = 65 - 27 = 6B5 - 2B7 = 4B-2 = 3B8 = 38$$

Alternatively, before subtracting we can create an overload outside by moving 1 tens from the inside to the outside as 10 1s

$$T = 65 - 27 = 6B5 - 2B7 = 5B15 - 2B7 = 3B8 = 38$$

Using bundle-writing to multiply 48 with 7 we get an overload outside the bundle allowing us to move 50 **1s** from the outside to the inside as 5 **tens**

$$T = 7*48 = 7*4B8 = 28B56 = 33B6 = 336$$

Alternatively, before multiplying we can create an underload outside by borrowing 2 **1s**. Later the underload can be removed by moving 2 **tens** outside as 20 **1s**

$$T = 7*48 = 7*4B8 = 7*5B-2 = 35B-14 = 33B6 = 336$$

Using bundle-writing to divide 336 with 7 we prefer to have 28 instead of 33 inside the bundle, so we create an overload outside by moving 5 bundles outside as 50 **1s**

$$T = 336 = 33$$
B $6 = 28$ **B** 56 ; so $T / 7 = 4$ **B** $8 = 48$

Alternatively, we can create an underload outside before dividing

$$T = 336 = 33B6 = 35B-14$$
; so $T / 7 = 5B-2 = 4B8 = 48$

To divide 338 by 7 we get 2 single leftovers that counted in 7s becomes a fraction 2/7

$$T = 338 = 33B8 = 28B58 = 28B56 + 2$$
; so $T / 7 = 4B8 + 2 / 7 = 482 / 7$

Introduction to the Chapters

Chapter 01, From Sticks to Icons, shows how rearranging four sticks creates a 4-icon with as many sticks as it represents; likewise with the other icons until ten having a name but no icon.

Chapter 02, Counting-sequences in Icons, shows that when counting by bundling, the bundle-icon is not used. Hence, when counting in tens, ten does not need an icon. A natural counting sequence will report both the bundles and the unbundled: 01, 02, ..., 10, 11; or 0.1, 0.2, ..., 1.0, 1.1 always including the bundle-name as the unit. Each bundle-size has its own counting sequence, but the standard is ten-counting in a sloppy version leaving out the unit and misplacing the decimal point by saying 23 instead of 2.3 tens.

Chapter 03, BundleCount in Icons, shows how a total T can be recounted in icon-bundles. Thus a total of nine things, represented by a line of sticks or beads on an abacus, can be counted in fours by a counting sequence. Also, they can be represented by a stack of bundles placed with one stick per bundle in a bundle that can written as a bracket (bundle-writing) and reported as a decimal number with a unit where the decimal point separates the bundles from the unbundled singles, T = 9 = 2B1 4s = 2.1 4s. Alternatively, a calculator can be asked to predict the counting result. Entering '9/4', we ask 'from 9, taking away 4s can be done how many times?' The calculator answers '2.some' so by entering '9 - 2x4' we ask 'from 9, once taking away 2 4s leaves what?' The answer '1' gives the calculator prediction T = 9 = 2.1 4s. Thus also operations are icons: /4 shows the broom wiping away 4 many times, – 4 shows the trace left when dragging away 4 only once, 2x shows the lifting needed to create a stack of 2 bundles, and +3 shows the juxtaposition of 3 singles left next to a stack of bundles. Moving 1 stick outside the bundle creates an overload T = 1B5 4s; and moving an extra stick in gives an underload, a deficit, T = 3B-3 4s. Thus by recounting, a total T of nine can be recounted in 4 different ways: T = nine = 9.1s = 2B1.4s = 1B5.4s = 3B-3.4s. This comes in handy when totals are added, subtracted, multiplied or divided. A good calculator says 2+3*4=14; a bad says 2+3*4=20.

Chapter 04, BundleCount with dices, shows how a total T can be recounted in icon-bundles where the total is shown on two similar dices and the icon-number is shown on a third dice.

Chapter 05, ReCount in the same Unit, shows how to recount a total T in the same unit by unbundling a bundle to singles thus creating an overload, or by borrowing extra singles that then has be counted for as a deficit. Thus a total of 2.1 5s can be written with overload as T = 1B6 5s or as T = 1.6 5s, or with borrowing as T = 3B-4 5s or as T = 3.-4 5s

Chapter 06, ReCount in a new Unit, shows how once counted in one unit, a total T can be recounted in another unit. Thus a total of 2 9s can be recounted in 6s as in chapter 3, again by lining, counting, bundling, stacking, bundle-writing and answering; and again checked by a calculator prediction using two formulas. The ReCount formula $\mathbf{T} = (\mathbf{T}/\mathbf{B}) * \mathbf{B}$ saying that 'from T, T/B times Bs can be taken away'; and the ReStack formula $\mathbf{T} = (\mathbf{T}-\mathbf{B}) + \mathbf{B}$ saying that 'From T, T-B is left when B is placed next to'. To change a unit is also called **proportionality**.

Chapter 07, ReCount in BundleBundles, shows how an overload in a bundle can be removed by an extra bundle for bundles-of-bundles. Thus counting a total T of 4 8s in 5s gives T = 6B2 5s. However, with 5 as the bundle-size, 5 bundles can be recounted as 1 bundle-of-bundles of 5s so that T = 6B2 5s = B1B2 5s = B1B2 5s or T = 6.2 5s = B1B2 5s.

Chapter 08, ReCount in Tens on Squared Paper or an Abacus, shows how easy totals counted in iconbundles can be recounted in tens since the calculator is programmed to give the answer directly in its sloppy version. Thus to recount 3 8s in tens we enter 3*8 and get the answer 24, so T = 3 8s = 2.4 tens. Recounting icon-numbers in tens systematically will provide the multiplication tables showing individual patterns in a ten by ten square or on an abacus.

Chapter 09, ReCount from Tens, shows, as in chapter 3, that we can get the answer through a calculator prediction or through lining, rebundling, and bundle-writing. Only this time we shorten the line by using Roman numbers as icons. Recounting large numbers from tens, we save time by using a multiplication table. Thus to recount a total T of 253 in 7s we use bundle-writing to create overloads guide by the table: T = 253 = 25B3 = 21B43 = 21B42 + 1 = 3B6 * 7 + 1, so T = 253 = 367s + 1.

Chapter 10, ReCount Large Numbers in Tens, show how bundle-writing may be used to create overloads later to be removed to get the final answer. Thus to recount 7 43s in tens gives a total T = 7.43s = 7*43 = 7*483 = 28B21 = 30B1 = 301 as confirmed by a calculator.

Chapter 11, DoubleCount with PerNumbers, shows that counting a quantity in two different physical units will provide a per-number to be used as a bridge connecting the two units. Thus counting a quantity as 4\$ and as 5 kg gives the per-number 4\$/5kg or 4/5 \$/kg. Asking '8\$ = ? kg', the answer comes from recounting the 8s in 4s to be able to use the per-number as a bridge between the two units: T = 8\$ = (8/4)*4\$ = (8/4)*5kg = 10kg. Likewise when asking e.g.'?\$ = 12kg'

Chapter 12, DoubleCount with Fractions and Percentages, shows that fractions and percentages can be treated as per-numbers. Thus asking '3/5 of 200\$' is the same as asking '3 per 5 of 200\$ gives?'. So we recount the 200 in 5s to get the answer: T = 200\$ = (200/5)*5\$ giving (200/5)*3\$ = 120\$. And asking '3% of 250\$' is the same as asking '3 per 100 of 250\$'. So we recount the 250 in 100s to get the answer: T = 250\$ = (250/100)*100\$ gives (250/100)*3\$ = 7.5\$ as confirmed by writing '3/100*250' on a calculator.

Chapter 13, ReCount PerNumbers, Fractions, shows how changing unit transforms per-numbers.

Chapter 14, Adding OnTop, shows that to add two totals T1 and T2 OnTop the units must be the same so recounting may be needed to change a unit. Thus adding 2 3s and 4 5s as 3s, the 4 5s must be recounted as 3s to give a total of 8.2 3s as confirmed by a calculator.

Chapter 15, Reversed Adding OnTop, shows that to reverse OnTop addition, the known total must be taken away before counting the rest in the unit of the second total. Thus asking '2 3s +? 5s total 5 3s, we take away the 2 3s from the 5 3s before recounting the rest, T - T1, in 5s by saying $(T-T1)/5 = \Delta T/5 = 1.4$ 5s as confirmed by a calculator. Subtraction followed by division is called differentiation.

Chapter 16, Adding NextTo, shows that adding two totals T1 and T2 NextTo means adding their areas, also called integration. Thus adding 2 3s and 4 5s NextTo each other as 8s on a ten by ten square or on an abacus gives 3.2 8s as confirmed by a calculator.

Chapter 17, Reversed Adding NextTo, shows that to reverse NextTo addition, the known total must be taken away before counting the rest in the unit of the second total. Thus asking '2 3s + ? 5s total 3 8s, we take away the 2 3s from the 3 8s before recounting the rest, T - T1, in 5s by saying $(T-T1)/5 = \Delta T/5 = 3.3$ 5s as confirmed by a calculator. Together, integration and differentiation is called **calculus**.

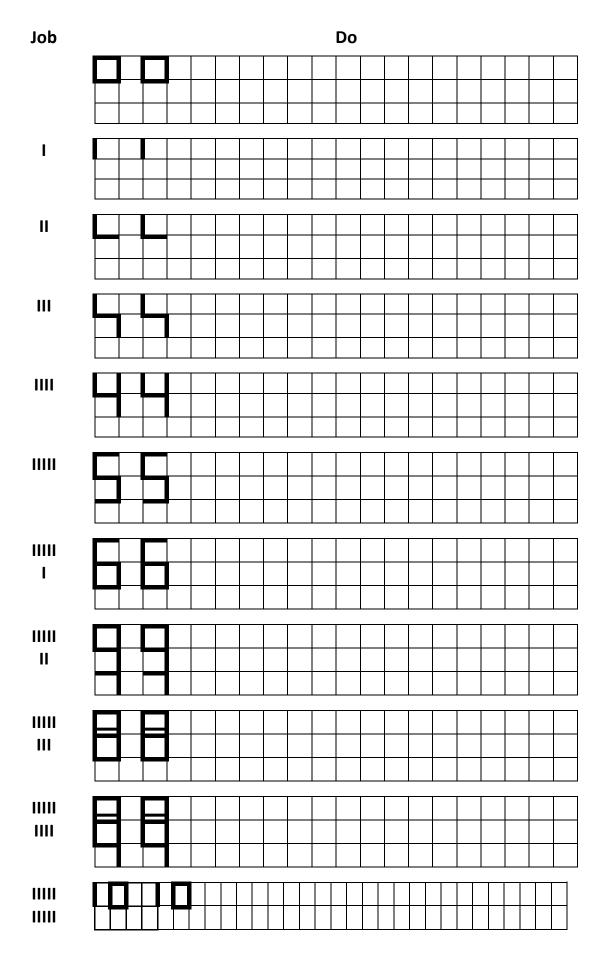
Chapter 18, Adding Tens, shows that when adding tens, bundle-writing can be used to create and remove overloads. Thus adding totals as 27 and 85 creates an overload that can be removed by bundle-writing, T = 27 + 85 = 2B7 + 8B5 = 10B12 = 11B2 = 112 as confirmed by a calculator.

Chapter 19, Reversed Adding Tens, the number added must be taken away which might result in a deficit calling for a unbundling a bundle, unless this is done first resulting in an overload that allows taking the number away without creating a deficit. Thus asking "? +27 = 85" or "85 - 27", bundle-writing is used to remove the deficit, 85 - 27 = 8B5 - 2B7 = 6B-2 = 5B8 = 58; or used to create an overload, 85 - 27 = 8B5 - 2B7 = 7B15 - 2B7 = 5B8 = 58, both confirmed by a calculator.

Chapter 20, Recounting Solves Equations, shows that equations expressing a reversed calculation can be solved by recounting and restacking. Thus to solve the equation $u^2 = 8$, 8 is recounted in 2s as $8 = (8/2)^2 = 4^2$, so that u = 4, checked by a calculator by entering 4^2 . With $u^2 = 8$ solved by u = 8/2 we get a shortcut for solving equations: *Move to the opposite side with the opposite sign*.

u*2	= 8 = (8/2)*2 = 4*2	Here we recount 8 in 2s as $8 = (8/2)*2 = 4*2$	u = 4
u+2	= 9 = (9-2)+2 = 7+2	Here we restack 9 to $9-2+2 = 7+2$	u = 7
u/3	= 2	Here we recount 2 in 3s as $2 = (2/3)*3 = 2*3/3 = 6/3$	u = 6
u-2	= 6	Here we restack 6 to $6-2+2=6+2-2=8-2$	u = 8
2*u+3	= 15	Here we restack 15 to $15-3+3=12+3$, and $2*u = 12 = 12/2*2 = 6*2$	u = 6
2*u-3	= 15	Here we restack 15 to $15-3+3=15+3-3=18-3$, and $2*u=18=18/2*2=9*2$	u = 9
u/2+3	= 15	Here we restack 15 to $15-3+3=12+3$, and $u/2 = 12 = 12/2*2 = 12*2/2 = 24/2$	u = 24
2/u-3	= 15	Here we restack 15 to $15-3+3=15+3-3=18-3$, and $2/u = 18 = 18/2*2 = 18*2/2 = 36/2$	u = 36

01. From Sticks to Icons



Count & Color Squares, Odd & Even

1		2			3			4			5			6			7			8			9		
								-									-								
9					8			7			6			5			4			3		2			1
2			4			6			8			1		3			5			7			9		
1		2			4			8			3			5			9				6			7	
3			6			9				8			5			4			7			1		2	
1		3			5			7			9				8			6			4			2	
5			3			1		2			4			7			9				8			6	

02. Counting-sequences in Icons

	ı	ı	ı	I	ı	I	ı	ı	ı	I	I	I	ı	ı
ten	1	2	3	4	5	6	7	8	9	10	11	12	13	14
ten	01	02	03	04	05	06	07	08	09	1B	1B1	1B2	1B3	1B4
ten	.1	.2	.3	.4	.5	.6	.7	.8	.9	1.	1.1	1.2	1.3	1.4
9	01	02	03	04	05	06	07	80	1B	1B1	1B2	1B3	1B4	1B5
9	.1	.2	.3	.4	.5	.6	.7	.8	1.	1.1	1.2	1.3	1.4	1.5
8														
8														
7														
7														
6														
6														
5														
5														
4														
4														
3	01	02	1B	1B1	1B2	2B	2B1	2B2	ВВ	1BB1	1BB2	1BB1B	1BB1B1	1BB1B2
3	.1	.2	1.	1.1	1.2	2.	2.1	2.2	10.	10.1	10.2	11.	11.1	11.2
2														
2														
11	1	2	3	4	5	6	7	8	9	Х	1B	1B1	1B2	1B3
11	01													
11	.1													

	II	II	II	П	II	П	Ш	Ш	Ш	П	Ш	Ш	II	II
ten	02				1B							2B2		
ten														
9														
9														
8														
8														
7														
7														
6														
6														
5														
5														
4														
3														
3														
	III	Ш	Ш	Ш	Ш									
ten														
9														
8														
7														
6														
5														
4														
3														
2														

03. BundleCount in Icons

Job		Do	Calcu	lator
	Line	T=	9/5	1.some
	Count	1, 2, 3, 4, B, 1B1, 1B2, 1B3, <u>1B4</u>	9 – 1*5	4
9	Bundle	T = 		·
in 5s	Stack		9 – 0*5	9
	B-write	T = 1B4 5s = 0B9 5s = 2B-1 5s	9-2*5	
	Answer	T = 9 = 1.4 5s		-
	Line	T=	9/4	2.some
	Count	1, 2, 3, B, 1B1, 1B2, 1B3, 2B, <u>2B1</u>	9 – 2*4	1
9	Bundle	T = 	3-24	1
in 4s	B-write	T = 2B1 4s = 1B5 4s = 3B-3 4s	9 – 1*4	5
	Stack		9-3*4	-3
	Answer	<u>T = 9 = 2.1 4s</u>		3
	Line			
	Count			
9	Bundle		9/	
in 3s	B-write		9 –	
	Stack			
	Answer			
	Line			
	Count			
8	Bundle		8	
in 4s	B-write		8	
	Stack			
	Answer			
	Line			
	Count			
8	Bundle		8	
in 3s	B-write		8	
	Stack			
	Answer			

	Line	
	Count	
7	Bundle	7
in 4s	B-write	7
	Stack	
	Answer	
	Line	
	Count	
6	Bundle	6
in 5s	B-write	6
	Stack	
	Answer	
	Line	
	Count	
5	Bundle	5
in 4s	B-write	5
	Stack	
	Answer	
	Line	
	Count	
4	Bundle	4
in 5s	B-write	4
	Stack	
	Answer	
	Line	
	Count	
3	Bundle	3
in 5s	B-write	3
	Stack	
	Answer	

04. BundleCount with Dices

Line			lator
	T=	0/4	2
Coun	1, 2, 3, B, 1B1, 1B2, 1B3, 2B, <u>2B1</u>	9/4 9 – 2*4	2.some
Bund	e T= 	9 – 2**4	1
B-wri	T = $2\mathbf{B}$ 1 4s = $1\mathbf{B}$ 5 4s = $3\mathbf{B}$ -3 4s	0 4*4	_
Stack		9-1*4	5
9 i 4s Answ	T = 9 = 2.1 4s	9 – 3*4	-3
Line			
Coun			
Bund	e	9/	
B-wri	re	9 –	
Stack			
Answ	er		
Line			
Coun			
Bund	e	9	
B-wri	re	9	
Stack			
Answ	er		
Line			
Coun			
Bund B-wri	e	7	
B-wri	re	7	
Stack			
Answ	er		
Line			
Line Coun			
Bund	е	7	
B-wri	re l	7	
Stack			
Answ	er		

Line	
Count	
Bundle	
B-write	
Stack	
Answer	
Line	
Count	
Bundle	
B-write	
Stack	
Answer	
Line	
Count	
Bundle	
B-write	
Stack	
Answer	
Line	
Count	
Bundle	
B-write	
Stack	
Answer	
Line	
Count	
Bundle	
B-write	
Stack	
Answer	

05. ReCount in the Same Unit

Job		Do	Bundle	Answer
	Line	T = IIIII IIIII I	2 B 1	T = 2.1 5s
2.1 5s	UnBundle	T =	1 B 6	T = 1.6 5s
in 5s	Embezzle	T = 11111 11111 11111	3 B -4	T = 34 5s
	Line			
2.1 4s	UnBundle			
in 4s	Embezzle			
	Line			
2.1 3s	UnBundle			
in 3s	Embezzle			
	Line			
2.1 6s	UnBundle			
in 6s	Embezzle			
	Line			
2.1 7s	UnBundle			
in 7s	Embezzle			
2.2.7	Line			
3.2 7s	UnBundle			
in 7s	Embezzle			
	Line			
3.2 6s	UnBundle			
in 6s	Embezzle			
	Line			
3.2 5s	UnBundle			
in 5s	Embezzle			
	Line			
3.2 4s	UnBundle			
in 4s	Embezzle			
2.2.5	Line			
3.2 3s	UnBundle			
in 3s	Embezzle			

	Line		
4.3 6s	UnBundle		
in 6s	Embezzle		
	Line		
4.3 5s	UnBundle		
in 5s	Embezzle		
	Line		
4.3 4s	UnBundle		
in 4s	Embezzle		
	Line		
5 7s	UnBundle		
in 7s	Embezzle		
	Line		
5 6s	UnBundle		
in 6s	Embezzle		
	Line		
5 4s	UnBundle		
in 4s	Embezzle		
	Line		
3 7s	UnBundle		
in 7s	Embezzle		
2.5-	Line		
3 5s	UnBundle		
in 5s	Embezzle		
4.2.6-	Line		
1.3 6s	UnBundle		
in 6s	Embezzle		
1.3 5s in 5s	Line		
	UnBundle		
	Embezzle		
1.3 4s	Line		
	UnBundle		
in 4s	Embezzle		

06. ReCount in a New Unit

Job		Do	Calculator	
	Line	T=		
	Count	1, 2, 3, 4, B, 1B1, 1B2, 1B3, 1B4,, <u>3B</u>		
2 9s	Bundle	T= 	2*9/6	3
in 6s	Stack		2*9 – 3*6	0
	B-write	T = 3 B		
	Answer	<u>T = 2 9s = 3 6s</u>		
	Line			
	Count			
2 9s	Bundle		2*9/	
in 5s	Stack		2*9 –	
	B-write			
	Answer			
	Line			
	Count			
2 8s	Bundle		2*8	
in 6s	Stack		2*8	
	B-write			
	Answer			
	Line			
	Count			
2 8s	Bundle		2*8	
in 5s	Stack		2*8	
	B-write			
	Answer			
	Line			
	Count			
2 7s	Bundle		2*7	
in 6s	Stack		2*7	
	B-write			
	Answer			

	Line	
	Count	
2 7s	Bundle	2*7
in 5s	Stack	2*7
111 33	B-write	
	Answer	
	Line	
	Count	
2 6s	Bundle	2*6
in 5s	Stack	2*6
	B-write	
	Answer	
	Line	
	Count	
2 6s	Bundle	2*6
in 4s	Stack	2*6
	B-write	
	Answer	
	Line	
	Count	
2 6s	Bundle	2*6
in 3s	Stack	2*6
	B-write	
	Answer	
	Line	
	Count	
2 5s	Bundle	5
in 4s	Stack	5
	B-write	
	Answer	

07. Recount in BundleBundles

Job		Do	Calculator
4 8s	B-write	T = 4 8s = 6B2 = B1B2 5s = 1B1B2	4*8/5 6.some
in 5s	Answer	<u>T = 4 8s = 6.2 5s = 11.2 5s = 123 5s</u>	4*8 – 6*5 2
5 8s	B-write		
in 6s	Answer		
6 9s	B-write		
in 7s	Answer		
9 9s	B-write		
in 8s	Answer		
3 9s	B-write		
in 4s	Answer		
4 5s	B-write		
in 3s	Answer		
6 8s	B-write		
in 5s	Answer		
6 8s	B-write		
in 4s	Answer		
7 8s	B-write		
in 5s	Answer		
7 8s	B-write		
in 4s	Answer		
8 8s	B-write		
in 5s	Answer		
8 8s	B-write		
in 4s	Answer		

7	B-write	T = 7 = 3 B 1 = B+1 B 1 = 1 B 1 B 1	7/2	3.some
in 2s	Answer	<u>T = 7 = 3.1 2s = 11.1 2s</u>	7 – 3*2	1
9	B-write	T = 9 = 4 B 1 = B+B B 1 = B B 0 B 1 = 1 B 0 B 0 B 1	9/2	4.some
in 2s	Answer	T = 9 = 4.1 2s = 20.1 2s = 100.1 2s	9 – 4*2	1
3 4s	B-write			
in 2s	Answer			
3 5s	B-write			
in 2s	Answer			
5 4s	B-write			
in 2s	Answer			
4 7s	B-write			
in 3s	Answer			
4 8s	B-write			
in 3s	Answer			
4 9s	B-write			
in 3s	Answer			
5 7s	B-write			
in 3s	Answer			
5 8s	B-write			
in 3s	Answer			
5 9s	B-write			
in 3s	Answer			
6 8s	B-write			
in 3s	Answer			
7 8s	B-write			
in 3s	Answer			

08. ReCount in Tens on Squared Paper or an Abacus

Job	Do	Calculator
7s	9 T	10 * 7 = 70 9 * 7 = 63 8 * 7 = 56 7 * 7 = 49 6 * 7 = 42
in tens	6 5 7 3 4 4 1	5 * 7 = 35 4 * 7 = 28 3 * 7 = 21 2 * 7 = 14 1 * 7 = 7
8s in tens		10 * 8 = 9 * 8 = 8 * 8 = 7 * 8 = 6 * 8 = 5 * 8 = 4 * 8 = 3 * 8 = 2 * 8 = 1 * 8 =
9s in tens		10 * 9 = 9 * 9 = 8 * 9 = 7 * 9 = 6 * 9 = 5 * 9 = 4 * 9 = 3 * 9 = 2 * 9 = 1 * 9 =
6s in tens		10 * 6 = 9 * 6 = 8 * 6 = 7 * 6 = 6 * 6 = 5 * 6 = 4 * 6 = 3 * 6 = 2 * 6 = 1 * 6 =

T	
	10 * 5 =
	9 * 5 =
	8 * 5 =
	7 * 5 =
5s	6 * 5 =
in tens	5 * 5 =
III tells	4 * 5 =
	3 * 5 =
	2 * 5 =
	1 * 5 =
	10 * 4 =
	9 * 4 =
	8 * 4 =
	7 * 4 =
4s	6 * 4 =
	5 * 4 =
in tens	4 * 4 =
	3 * 4 =
	2 * 4 =
	1 * 4 =
	10 * 3 =
	9 * 3 =
	8 * 3 =
20	7 * 3 =
3s	6 * 3 =
in tens	5 * 3 =
	4 * 3 =
	3 * 3 =
	2 * 3 =
	1 * 3 =
	10 * 2 =
	9 * 2 =
	8 * 2 =
	7 * 2 =
2s	6 * 2 =
in tens	5 * 2 =
	4 * 2 =
	3 * 2 =
	2 * 2 =
	1 * 2 =
1	 l .

09. Recount From Tens

Job		Do	Calcu	lator
	Line	XXXVII		
37	ReBundle	9 9 9 V -> 9 9 9 X -> 9 9 9 1	37/9	4.some
in 9s	B-write	3B 7 = B37 = B36 + 1 = B4*9 + 1	37 – 4*9	1
	Answer	<u>T = 37 = 4*9 + 1 = 4.1 9s = 4 1/9 9s</u>		
	Line			
37	ReBundle			
in 7s	B-write			
	Answer			
	Line			
37	ReBundle			
in 5s	B-write			
	Answer			
	Line			
42	ReBundle			
in 7s	B-write			
	Answer			
	Line			
42	ReBundle			
in 5s	B-write			
	Answer			
	Line			
26	ReBundle			
in 7s	B-write			
	Answer			
	Line			
26	ReBundle			
in 5s	B-write			
	Answer			

253	B-write	T = 2 B 5 B 3 = 25 B 3 = 21 B 43 = 21 B 42 + 1	253/7	36.some
in 7s	Answer	T = 3 B 6 * 7 + 1 = 36 * 7 + 1 = <u>36 1/7 7s</u>	253 – 36*7	1
253	B-write			
in 9s	Answer			
253	B-write			
in 5s	Answer			
253	B-write			
in 3s	Answer			
842	B-write			
in 7s	Answer			
842	B-write			
in 5s	Answer			
842	B-write			
in 4s	Answer			
842	B-write			
in 2s	Answer			
904	B-write			
in 8s	Answer			
904	B-write			
in 7s	Answer			
904	B-write			
in 5s	Answer			
904	B-write			
in 3s	Answer			
789	B-write			
in 8s	Answer			
789	B-write			
in 7s	Answer			
789	B-write			
in 5s	Answer			
789	B-write			
in 4s	Answer			

10. Recount Large Numbers in Tens

Job		Do	Calculat	or
	B-write	T = 7 * 4B3 = 28B21 = 30B1 = 301	7*43	201
7 43s	Answer	<u>T = 7 43s = 30.1 tens = 301</u>	7*43	301
	B-write			
8 43s	Answer			
	B-write			
9 43s	Answer			
	B-write			
6 43s	Answer			
	B-write			
5 62s	Answer			
	B-write			
4 62s	Answer			
	B-write			
3 62s	Answer			
	B-write			
2 62s	Answer			
	B-write			
27 436s	Answer			
2.426	B-write			
3 436s	Answer			
	B-write			
4 436s	Answer			
	B-write			
5 436s	Answer			
	B-write			
6 436s	Answer			
	B-write			
7 436s	Answer			
	B-write			
8 436s	Answer			

	B-write	T = 17 * 4 B 3 = 68 B 51 = 73 B 1 = 731	47440	704
17 43s	Answer	<u>T = 17 43s = 73.1 tens = 731</u>	17*43	731
	B-write			
27 43s	Answer			
	B-write			
37 43s	Answer			
	B-write			
47 43s	Answer			
	B-write			
57 43s	Answer			
	B-write			
67 43s	Answer			
	B-write			
77 43s	Answer			
	B-write			
87 43s	Answer			
22.242	B-write	T = 32 * 2 B 4 B 3 = 64 B 128 B 96	32*243 7	7776
32 243s				1110
32 2435	Answer	= 64 B 137 B 6 = 77 B 7 B 6 = 777.6 tens = 7776		
	Answer B-write	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s		= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s	B-write	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
	B-write Answer	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s 43 343s	B-write Answer B-write	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s	B-write Answer B-write Answer	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s 43 343s 56 453s	B-write Answer B-write Answer B-write	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s 43 343s	B-write Answer B-write Answer B-write Answer	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s 43 343s 56 453s 62 637s	B-write Answer B-write Answer B-write Answer B-write	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s 43 343s 56 453s	B-write Answer B-write Answer B-write Answer B-write Answer	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s 43 343s 56 453s 62 637s 74 843s	B-write Answer B-write Answer B-write Answer B-write Answer B-write Answer	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s 43 343s 56 453s 62 637s	B-write Answer B-write Answer B-write Answer B-write Answer B-write Answer Answer	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		
35 413s 43 343s 56 453s 62 637s 74 843s	B-write Answer B-write Answer B-write Answer B-write Answer B-write Answer B-write Answer	= 64B137B6 = 77B7B6 = 777.6 tens = 7776		

11. DoubleCount with PerNumbers

Job	Do	Formula
With 4 \$ per 5 kg		Kg = (kg/\$)*\$
8\$ = ?kg	8\$ = (8/4)*4\$ = (8/4)*5kg = 10kg	Kg = (5/4)*8 = 10
?\$ = 12 kg	12kg = (12/5)*5kg = (12/5)*4\$ = 9.6\$	\$ = (\$/kg)*kg \$ = (4/5)*12 = 9.6
With 3 \$ per 5 kg		
8\$ = ?kg		
?\$ = 12 kg		
With 4 \$ per 6 kg		
8\$ = ?kg		
?\$ = 12 kg		
With 4 \$ per 8 kg		
8\$ = ?kg		
?\$ = 12 kg		
With 4 \$ per 5 kg		
8\$ = ?kg		
?\$ = 12 kg		
With 3 \$ per 5 kg		
8\$ = ?kg		
?\$ = 12 kg		
With 4 \$ per 6 kg		
8\$ = ?kg		
?\$ = 12 kg		
With 4 \$ per 8 kg		
8\$ = ?kg		
?\$ = 12 kg		
With 2 \$ per 5 kg		
8\$ = ?kg		
?\$ = 12 kg		
With 2 \$ per 7 kg		
8\$ = ?kg		
?\$ = 12 kg		

12. DoubleCount with Fractions and Percentages

Job	Do	Calculator	
3 per 5 of 200\$	200\$ = (200/5)*5\$		
	Giving (200/5)*3\$ = 120\$	3/5*200	120
3 per 5 of 400\$			
2 per 5 of 200\$			
1 per 5 of 200\$			
3 per 6 of 240\$			
2 per 6 of 240\$			
5 per 6 of 300\$			
3 per 100 of 250\$	250\$ = (250/100)*100\$		
or 3% of 250\$	Giving (250/100)*3\$ = 7.5\$	3/100*250	7.5
8 per 100 of 200\$			
or 8% of 200\$			
20 per 100 of 200\$			
or 20% of 200\$			
3 per 100 of 560\$			
or 3% of 560\$			
8 per 100 of 560\$			
or 8% of 560\$			
12 per 100 of 560\$			
or 12% of 560\$			
20 per 100 of 560\$			
or 20% of 560\$			
60 per 100 of 560\$			
or 60% of 560\$			

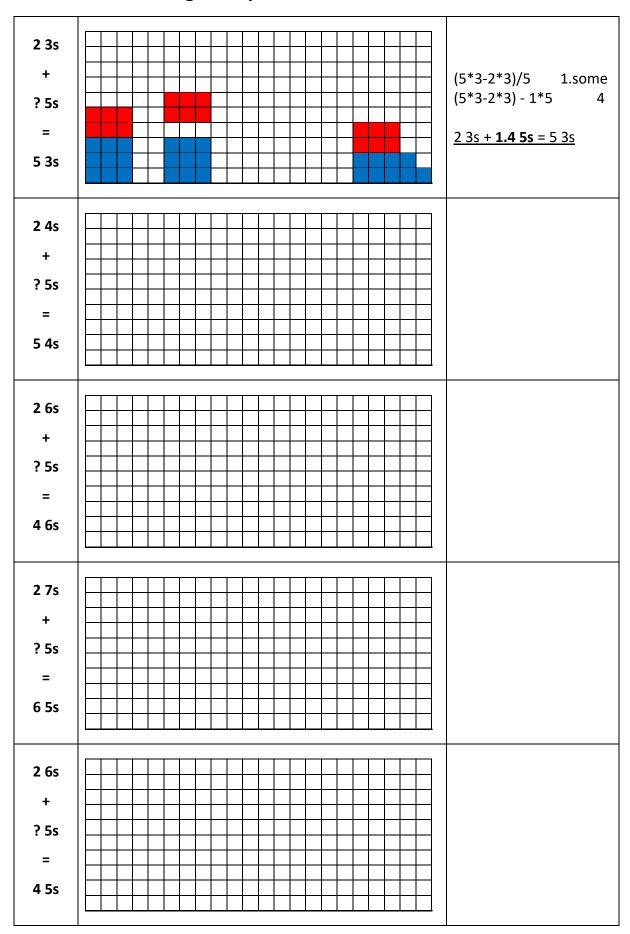
13. ReCount PerNumbers, Fractions

Job	Do	Do	Calculator	Calculator
2/3	2/3 = 2 2s / 3 2s = 4/6	2/3 = 2 4s / 3 4s = 8/12	2/3 = 0.66	8/12 = 0.66
= ?	2/3 = 2 3s / 3 3s = 6/9	2/3 = 2 5s / 3 5s = 10/15	4/6 = 0.66	10/15 = 0.66
1/3				
= ?				
1/5				
= ?				
2/5 = ?				
3/5				
= ?				
4/5				
= ?				
4/6	4/6 = 2 2s / 3 2s = 2/3	6/8 = 3 2s / 4 2s = 3/4	4/6 = 0.66	6/8 = 0.75
2/6			2/3 = 0.66	3/4 = 0.75
6/8	2/6 = 1 2s / 3 2s = 1/3	2/8 = 1 2s / 4 2s = 1/4	2/6 = 0.33	2/8 = 0.25
2/8			1/3 = 0.33	1/4 = 0.25
2/10 4/10				
6/10				
8/10				
2/12				
4/12				
6/12				
8/12				
10/12				
2/14				
4/14 6/14				
8/14				
10/14				
12/14				
2/16				
4/16				
6/16				
8/16				
10/16				
12/16				
14/16				

14. Add OnTop

Job	Do	Calculator
2 3s		
+		(2*3+4*5)/3 8.some
		(2*3+4*5) - 8*3 2
4 5s		<u>2 3s + 4 5s = 8.2 3s</u>
=		(2*3+4*5)/5 5.some
? 3s		(2*3+4*5) - 5*5 1
? 5s		2 3s + 4 5s = 5.1 5s
2 4s		
+		
3 5s		
=		
? 4s		
? 5s		
3 2s		
+		
4 6s		
=		
? 2s		
? 6s		
2 5s		
+		
4 3s		
=		
? 5s		
? 3s		
5 2s		
+		
3 4s		
=		
? 2s		
? 4s		

15. Reversed Adding OnTop

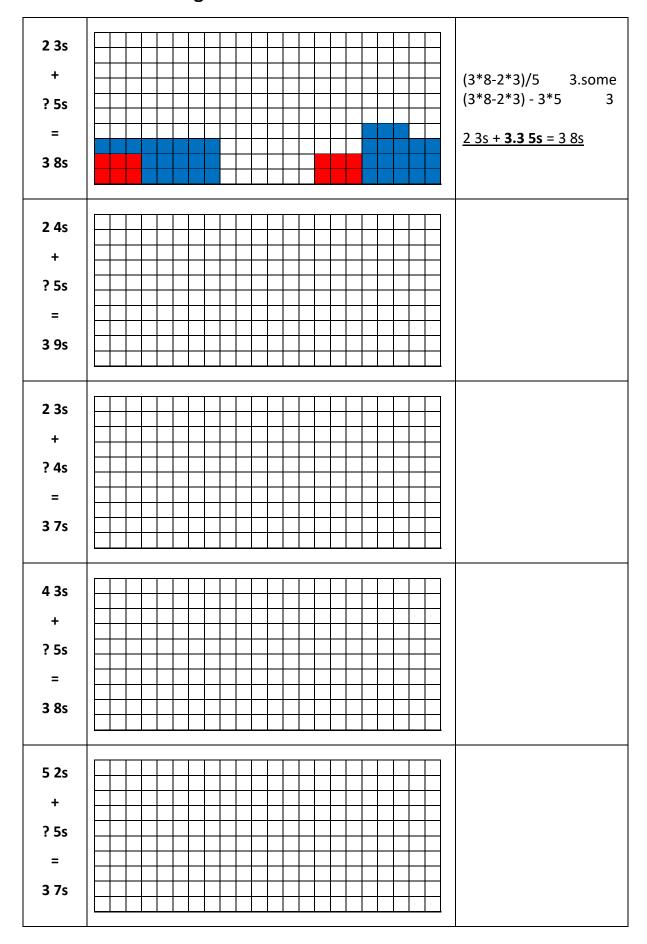


16. Add NextTo

Job	Do	Calculator
2 3s + 4 5s = ? 8s		(2*3+4*5)/8 3.some (2*3+4*5) - 8*3 2 2 3s + 4 5s = 3.2 8s
3 2s + 4 5s = ? 7s		
2 3s + 4 6s = ? 9s		
2 4s + 4 5s = ? 9s		
4 3s + 2 4s = ? 6s		

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17. Reversed Adding NextTo



18. Add Tens

Job		Do	Calculate	or
	B-write	T = 2B7 + 8B5 = 10B12 = 11B2 = 112	27.05	112
27 + 85	Answer	<u>T = 27 + 85 = 11.2 tens = 112</u>	27+85	112
	B-write			
27 + 85	Answer			
	B-write			
33 + 78	Answer			
	B-write			
39 + 71	Answer			
	B-write			
45 + 67	Answer			
	B-write			
58 + 57	Answer			
	B-write			
57 + 49	Answer			
	B-write			
27 + 205	Answer			
	B-write			
33 + 198	Answer			
	B-write			
39 + 191	Answer			
4- 40-	B-write			
45 + 187	Answer			
	B-write			
58 + 177	Answer			
	B-write			
57 + 169	Answer			
	B-write			
127 + 385	Answer			
400	B-write			
433 + 578	Answer			

19. Reversed Adding Tens

Job		Do	Calculator
	B-write	D = 8 B 5 – 2 B 7 = 6 B -2 = 5 B 8 = 58	
27 + ? = 85		D = 8B5 - 2B7 = 7B15 - 2B7 = 5B8 = 58	85 – 27 58
85 – 27	Answer	<u>T = 85 – 27 = 5.8 tens = 58</u>	
	B-write		
63 – 17			
	Answer		
	B-write		
55 – 36			
	Answer		
	B-write		
35 – 17			
	Answer		
	B-write		
185 – 27			
	Answer		
	B-write		
235 – 128			
	Answer		
	B-write		
242 – 128			
	Answer		
	B-write		
245 – 167			
	Answer		
	B-write		
312 – 159			
	Answer		
	B-write		
421 – 268			
	Answer		

20. ReCounting solves Equations

Do	Equation	Calcu	Calculator	
ReCount	u*2 = 30 = (30/2)*2 = 15*2	15*2	20	
Answer	u = 15	15*2	30	
ReCount	u*3 = 15			
Answer				
ReCount	u*4 = 32			
Answer				
ReCount	u*5 = 40			
Answer				
ReCount	u/3 = 12 = (12/3)*3 = 12*3/3 = 36/3	26/2	12	
Answer	u = 36	36/3	12	
ReCount	u/3 = 10			
Answer				
ReCount	u/4 = 8			
Answer				
ReCount	u/5 = 6			
Answer				
ReCount	u+2 = 30 = (30-2)+2 = 28 + 2	20.2	20	
Answer	u = 28	28+2	30	
ReCount	u+3 = 24			
Answer				
ReCount	u+4 = 20			
Answer				
ReCount	u+5 = 12			
Answer				
ReCount	u-2 = 30 = (30-2)+2 = 30+2-2 = 32-2	22.2	20	
Answer	u = 32	32-2	30	
ReCount	u-3 = 20			
Answer				
ReCount	u-5 = 10			
Answer				

ReCount	2*u+3 = 15 = (15-3)+3 = 12 + 3		
ReCount	2*u = 12 = (12/2)*2 = 6*2	2*6+3	15
Answer	u = 6		
ReCount	3*u+4 = 19		
ReCount			
Answer			
ReCount	4*u+6 = 38		
ReCount			
Answer			
ReCount	2*u-3 = 15 = (15-3)+3 = 15+3-3 = 18 - 3		
ReCount	2*u = 18 = (18/2)*2 = 9*2	2*9-3	15
Answer	u = 9		
ReCount	3*u-4 = 8		
ReCount			
Answer			
ReCount	4*u-5 = 23		
ReCount			
Answer			
ReCount	u/2+3 = 15 = (15-3)+3 = 12 + 3		
ReCount	u/2 = 12 = (12/2)*2 = (12*2)/2 = 24/2	24/2+3	15
Answer	u = 24		
ReCount	u/3+4= 12		
ReCount			
Answer			
ReCount	u/2-3 = 15 = (15-3)+3 = (15+3)-3 = 18 - 3		
ReCount	u/2 = 18 = (18/2)*2 = (18*2)/2 = 36*2	36/2-3	15
Answer	u = 36		
ReCount	u/4-7 = 5		
ReCount			
Answer			