

Proposals for Papers

Invitation to Co-authorship

Allan.Tarp@MATHeCADEMY.net

February 2020

STEM prevents a goal-displacement that makes mathematics a goal instead of a means.....	1
Stop teaching wrong numbers and operations, start guiding children's mastery of many	2
To support STEM, trigonometry and coordinate geometry should precede plane geometry.....	3
A fresh-start year10 (pre)calculus curriculum.....	4
To support STEM, calculus must teach adding bundle-numbers, per-numbers and fractions also...	5
Conflicting grand theories create 2x3x2 different mathematics educations	6
Replacing STEAM with STE3M will include also economics and English	7
The power of per-numbers	8
Mixing design and difference research with experiential learning cycles allows creating classroom teaching for all students	9
From place value to bundle-bundles: units, decimals, fractions, negatives, proportionality, equations and calculus in grade one	10
Sociological imagination designs micro-curricula for experiential learning cycles	11
Concrete STEM subjects allow mathematics learning by modeling and peer-brain teaching	12
The simplicity of mathematics designing a stem-based core curriculum for refugee camps	13

STEM PREVENTS A GOAL-DISPLACEMENT THAT MAKES MATHEMATICS A GOAL INSTEAD OF A MEANS

Allan Tarp

MATHeCADEMY.net

Asking what is the purpose of mathematics education, US and UK mathematics educators say “to learn school mathematics”. Others say “to learn set-based mathematics as defined by university mathematics.” Focusing on competences leads to saying “to learn mathematical competences” or “to master mathematics”. Seldom, if ever, is heard that the goal is “to master many” or “to develop the number-language that children bring to school.”

Sociological imagination (Bauman, 1990) may prevent a goal displacement where a means becomes a goal instead. Historically, the Pythagoreans chose the word ‘mathematics’ meaning ‘knowledge’ in Greek as a common name for their knowledge about Many in space and time and by itself: astronomy, music, geometry and arithmetic. And today in North America, mathematics is still a common name for geometry and algebra, showing their outside goals in their original meanings, earth-measuring in Greek, and reuniting in Arabic. Integration and differentiation also name their tasks directly, to integrate small changes, and to differentiate a total change in small changes.

To avoid a goal displacement, mathematics must de-model (Tarp, 2019) its core ingredients: digits, operations, equations, fractions, functions etc. to allow primary school develop the flexible bundle-numbers children bring to school by teaching, not numbers to add, but numbering totals by counting, recounting and double-counting, where recounting 8 fingers in 2s as $8 = (8/2)*2$ leads directly to the recount-formula $T = (T/B)*B$ with per-numbers that solve equations, that occur in most STEM-formulas typically predicting proportionality, and that become fractions when double-counting in the same unit.

Liberated from its goal displacement, mathematics education may have its own communicative turn as in the 1970s (Widdowson, 1978) such that from now on both the word- and the number-language are taught and learned through their use and not through their grammar, thus allowing all students to model outside quantities as to levels, change and distribution.

References

- Bauman, Z. (1990). *Thinking sociologically*. Oxford, UK: Blackwell.
- Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.
- Tarp, A. (2019). *De-modeling numbers, operations and equations: from inside-inside to outside-inside understanding*. Proceedings from Psychology and Mathematics education conference at the Ho Chi Minh City University of Education on December 7, 2019.
- Widdowson, H. G. (1978). *Teaching language as communication*. Oxford, UK: Oxford University Press.

STOP TEACHING WRONG NUMBERS AND OPERATIONS, START GUIDING CHILDREN'S MASTERY OF MANY

Allan Tarp

MATHeCADEMY.net

Learning means adapting the inside brain to outside nature and culture. Vygotsky prioritizes culture and wiser-brain teaching, Piaget nature and peer-brain learning.

Adapting to Many, children answer the question 'How many?' with bundle-numbers as $T = 2 \text{ } 3s$ containing two digits: 3 is a quantity-number in space, also called a cardinal-number taking on positive integer values; 2 is a counting-number in time taking on also decimal, fractional, and negative values as $T = 7 = 2.1 \text{ } 3s = 2 \frac{1}{3} \text{ } 3s = 3.-2 \text{ } 3s$.

Quantity-numbers may add, and so may counting-numbers, but not in between. So, digits must be categorized before adding. Digits are not numbers but operators, needing a multiplier to become a number, $T = 2 \text{ } 3s = 2*3$, as seen when writing numbers fully as polynomials, as e.g. $T = 345 = 3*B^2 + 4*B + 5*1$

So, teaching digits as numbers is teaching wrong numbers. And bundle-numbers need not to be taught since children bring them to school, that should guide them to develop their number-language by learning that

- digits are icons with as many strokes as they represent.
- operations are icons also, rooted in the counting process: division is a broom pushing away bundles, multiplication is a lift stacking bundles, subtraction is a rope pulling away stacks to find unbundled, and addition is the two ways to unite stacks, on-top and next-to.
- recounting 8 in 2s gives a recount-formula: $8 = (8/2)*2$, or $T = (T/B)*B$, used to solve the equation $u*2 = 8$ by recounting 8 in 2s to give the solution $u = 8/2$; thus solving most STEM-equations, typically predicting proportionality.

Later recounting between digit-units and tens leads to tables, and to equations when asking e.g. $T = 4 \text{ } 6s = ? \text{ } \text{tens}$, and $T = 42 = 4.2 \text{ } \text{tens} = ? \text{ } 7s$.

So, childhood education should guide children develop the quantitative competence they bring to school using Kolb's experiential learning cycles.

References

Kolb, D. (1983). *Experiential learning*. New Jersey: Prentice Hall.

Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.

TO SUPPORT STEM, TRIGONOMETRY AND COORDINATE GEOMETRY SHOULD PRECEDE PLANE GEOMETRY

Allan Tarp

MATHeCADEMY.net

Halved by its diagonal c , a rectangle becomes a right triangle ABC with base b and height h . Using the recount-formula $T = (T/B)*B$ coming from recounting 8 in 2s as $8 = (8/2)*2$, mutual recounting gives trigonometry: $h = (h/c)*c = \sin A * c$, $b = (b/c)*c = \cos A * c$, $h = (h/b)*b = \tan A * b$.

Splitting the diagonal in $c1$ and $c2$ by the triangle-height produces two triangles where $\cos A = c1/b = b/c$, making $b^2 = c*c1$, and $\cos B = c2/h = h/c$, making $h^2 = c*c2$, thus giving the Pythagoras rule $h^2 + b^2 = c^2$.

Finding $\sqrt{70}$ means squeezing 7 tens until becoming a square $(8+t)^2$ situated between 8^2 and 9^2 . And having four parts as shown by two playing cards placed like an L: 8^2 , and $8*t$ twice, and t^2 . Neglecting t^2 , we get the equation $8*t = (70-8^2)/2 = 3 = (3/8)*8$, solved by recounting 8 in 3s, giving $t = 3/8 = 0.375$, so $8.375^2 = 70,14 = 70$ approximately.

In a coordinate system, a circle with center in the origin and radius r gets the equation $x^2 + y^2 = r^2$, else $(\Delta x)^2 + (\Delta y)^2 = r^2$. In a horizontal right triangle, moving along the diagonal will change x and y with Δx and Δy . Recounting Δy in Δx gives $\Delta y = (\Delta y/\Delta x)*\Delta x = m*\Delta x = \tan A *\Delta x$ that allows drawing lines from tables.

Intersection points between lines are predicted by a linear equation solved by technology or by moving to opposite side with opposite sign.

Intersection points between lines and circles or parabolas are predicted by a quadratic equation $x^2 + b*x + c = 0$, solved by two L-placed playing cards showing that $(x+t)^2 = x^2 + 2*x*t + c + (t^2 - c)$ where the first three terms disappear with $t = b/2$.

References

Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.

A FRESH-START YEAR10 (PRE)CALCULUS CURRICULUM

Allan Tarp

MATHeCADEMY.net

Often precalculus suffers from lacking student knowledge. Three options exist: make mathematics non-mandatory, choose an application-based curriculum; or, to rebuild student self-confidence, design a fresh-start curriculum that also includes the core of calculus by presenting integral calculus first.

Writing a number out fully as a polynomial, e.g. $T = 345 = 3*B^2 + 4*B + 5$ shows the four ways to unite numbers, resonating with the Arabic meaning of the word algebra, to reunite: addition and multiplication unite changing and constant unit-numbers into totals; and next-to-block-addition (integration) and power unite changing and constant per-numbers, all having reverse operations that split totals into parts.

Addition, multiplication, and power are defined as counting-on, repeated addition and repeated multiplication. As reverse operations, $x = 7-3$ is defined as the number that added to 3 gives 7, thus solving the equation $x+3 = 7$ by moving to opposite side with opposite sign. Likewise, $x = 7/3$ solves $x*3 = 7$, the factor-finder (root) $x = 3\sqrt[3]{7}$ solves $x^3 = 7$, and the factor-counter (logarithm) $x = \log_3(7)$ solves $3^x = 7$, again moving to opposite side with opposite sign.

Hidden brackets allow reducing a double calculation to a single: $2+3*x = 14$ becomes $2+(3*x) = 14$, solved by $x = (14-2)/3$. Next transposing letter-equations as $T = a+b*c^d$ really boost self-pride.

Future behavior of 2set unit-number tables is predicted by linear, exponential, or power models assuming constant change-number, change-percent, or elasticity.

1-4set per-number speed tables are modeled with lines, parabolas and double-parabolas, allowing technology to calculate the distance covered, thus introducing integral calculus, that also occurs when adding per-numbers in mixture-problems, and when adding percent in cross tables generated by statistical questionnaires.

Trigonometry comes from mutual double-counting sides in a rectangle halved by its diagonal, and is used to model distances to far away points, bridges, roads on hillsides, motion down an incline, and jumps from a swing.

References

Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.

TO SUPPORT STEM, CALCULUS MUST TEACH ADDING BUNDLE-NUMBERS, PER-NUMBERS AND FRACTIONS ALSO

Allan Tarp

MATHeCADEMY.net

Created to add locally constant per-numbers by their areas, integral calculus normally is the last subject in high school, and only taught to a minority of students. But, since most STEM-formulas express proportionality by means of per-numbers, the question is if integral calculus may be taught earlier. Difference research searching for hidden differences finds that the answer is yes.

Integral calculus occurs in grade one when performing next-to addition of bundle-numbers as e.g. $T = 2 \text{ 3s} + 4 \text{ 5s} = ? \text{ 8s}$, leading on to differential calculus as the reverse question: $2 \text{ 3s} + ? \text{ 5s} = 3 \text{ 8s}$, solved by first removing 2 3s from 3 8s and then counting the rest in 5s , thus letting subtraction precede division, where integral calculus does the opposite by letting multiplication creating areas precede addition.

In middle school adding per-numbers by areas occurs in mixture problems: $2\text{kg at } 3\$/\text{kg} + 4\text{kg at } 5\$/\text{kg} = 6\text{kg at } ? \$/\text{kg}$, again with differential calculus coming from the reverse question: $2\text{kg at } 3\$/\text{kg} + 4\text{kg at } ? \$/\text{kg} = 6\text{kg at } 5 \$/\text{kg}$. Here the per-number graph is piecewise constant c , i.e. there exists a delta-interval so that for all positive epsilon, the distance between y and c is less than epsilon. With like units, per-numbers become fractions thus also added by their areas, and never without units.

In high school adding per-numbers occurs when the meters traveled with varying m/s speed P is found as the area under the per-number graph now being locally constant, formalized by interchanging epsilon and delta. Here the area A under the per-number graph P , is found by slicing the area thinly so that its change may be written as $dA = P \cdot dx$ in order to use that when differences add, all middle terms disappear leaving just the endpoint difference, thus motivating developing differential calculus to find $A' = dA/dx = P$.

References

- Tarp, A. (2017). *Difference-research powering PISA performance: count & multiply before you add*. Keynote presentations to the CTRAS 2017 conference in Dalian, China.
- Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.

CONFLICTING GRAND THEORIES CREATE 2X3X2 DIFFERENT MATHEMATICS EDUCATIONS

Allan Tarp

MATHeCADEMY.net

As part of institutionalized education, mathematics falls under the focus of the three grand theories, philosophy, sociology and psychology, discussing different kinds of mathematics, of education and of learning; and recommending appropriate means to institutional goals. However, is the goal to master mathematics first, as a means to later master many; or to master many directly if mastering mathematics proves difficult?

As to learning, psychology sees coping coming from brains adapting to outside nature and culture, but which is more important? Vygotsky points to culture, mediated by a more knowledgeable wiser-brain, a teacher. Piaget points to nature, automatically creating inside schemata that accommodate if meeting outside resistance from nature or from peer-brain communication.

As to mathematics, philosophy has three conflicting views: Pre-modern mathematics is inspired by the Pythagoreans seeing mathematics as knowledge about Many in space and time and by itself as expressed in astronomy, music, geometry and arithmetic; and as part of the three basic Rs: reading, writing and 'rithmetic called reckoning in Germanic countries. Modern mathematics needs no outside examples for its concepts. Alternatively, postmodern scepticism sees mathematics as a number-language abstracting inside concepts from outside examples, and parallel to the word-language.

As to institutions, sociology recommends imagination to prevent a goal displacement making a means a goal instead. As to education, two conflicting views exists. One sees the student as a servant of the state forcing its population to choose between different multiyear tracks from upper secondary school, and forcing students back to start if changing track. One sees the state as a servant of the student by helping students to uncover and develop their personal talent in self-chosen half-year blocks after puberty.

So, two different learning forms, three different mathematics forms, and two different education forms create 2x3x2 different ways of conducting mathematics education.

References

- Bauman, Z. (1990). *Thinking sociologically*. Oxford, UK: Blackwell.
- Foucault, M. (1995). *Discipline & punish*. New York, NY: Vintage Books.
- Freudenthal, H. (1973). *Mathematics as an educational task*. Dordrecht, Holland: D. Reidel Publishing Company.
- Hobbes, T. (2019). *Leviathan*. London, UK: Penguin Classics.
- Locke, J. (2008). *An essay concerning human understanding*. Oxford, UK: Oxford World's Classics.
- Piaget, J. (1969). *Science of education of the psychology of the child*. New York, NY: Viking Compass.
- Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.
- Vygotsky, L. (1986). *Thought and language*. Cambridge, MA: MIT press.

REPLACING STEAM WITH STE3M WILL INCLUDE ALSO ECONOMICS AND ENGLISH

Allan Tarp

MATHeCADEMY.net

STEM integrates mathematics with its roots in science, technology and engineering, all using formulas from algebra and trigonometry to pre-dict the behavior of physical quantities. Statistics post-dicts unpredictable quantities by setting up probabilities for future behavior, using factual or fictitious numbers as median and fractals or average and deviation. Including economics and English in STEM opens the door to statistics also. Art may be an appetizer, but not a main course since geometry and algebra should be always together and never apart to play a core role in STEM.

Macroeconomics describes households and factories exchanging salary for goods on a market in a cycle having sinks and sources: savings and investments controlled by banks and stock markets; tax and public spending on investment, salary and transferals controlled by governments; and import and export controlled by foreign markets experiencing inflation and devaluation. Proportionality and linear formulas may be used as first and second order models for this economic cycle, using regression to set up formulas and spreadsheet for simulations using different parameters.

Microeconomics describes equilibriums in the individual cycles. On a market, shops buy and sell goods with a budget for fixed and variable cost, and with a profit depending on the volume sold and the unit-prices, all leading to linear equations. In the case of two goods, optimizing leads to linear programming. Competition with another shop leads to linear Game Theory. Market supply and demand determines the equilibrium price. Market surveys leads to statistics, as does insurance. In the households, spending comes from balancing income and transferals with saving and tax. In a bank, income come from simple and compound interest, from installment plans as well as risk taking. At a stock market, courses fluctuate. Governments must consider quadratic Laffer-curves describing a negative return of a tax-raise. To avoid units, factories use variations of Cobb-Douglas power elasticity production functions for modeling.

In English sentences may be analyzed on a word level as to the frequency of subjects, verbs, direct and indirect objects, predicates, and unspecified words.

References

- Galbraith, J. K. (1987). *A history of economics*. London: Penguin Books.
- Heilbroner, R. & Thurow, L. (1998). *Economics explained*. New York: Touchstone.
- Keynes, J. M. (1973). *The general theory of employment, interest and money*. Cambridge: University Press.
- Screpanti, E. & Zamagni, S. (1995). *An outline of the history of economic thought*. Oxford: University Press.
- Tarp, A. (2001). Fact, fiction, fiddle - three types of models. in J. F. Matos, W. Blum, K. Houston & S. P. Carreira (Eds.), *Modelling and mathematics education. ICTMA 9: Applications in Science and Technology. Proceedings of the 9th International Conference on the Teaching of Mathematical Modelling and Applications* (pp. 62-71). Chichester, UK: Horwood Publishing.

THE POWER OF PER-NUMBERS

Allan Tarp

MATHeCADEMY.net

Uniting unit-numbers as 4\$ and 5\$, or per-numbers as 6\$/kg and 7\$/kg or 6% and 7%, we observe that addition and multiplication unite changing and constant unit-numbers into a total, and integration and power unite changing and constant per-numbers. Reversely, subtraction and division split a total into changing and constant unit-numbers, and integration and power split a total into changing and constant per-numbers.

Recounting 8 in 2s as $8 = (8/2)*2$ creates a recount-formula $T = (T/B)*B$, saying ‘From T, T/B times, T may be pushed away’; and used to change units when asking e.g. 2 6s = ? 3s, giving the prediction $T = (2*6/3)*3 = 4*3 = 4$ 3s.

Recounting 8 in 2s also provides the solution $u = 8/2$ to the equations as $u*2 = 8 = (8/2)*2$; thus solving most STEM-equations, since the recount-formula occurs all over. In proportionality, $y = c*x$; in coordinate geometry as line gradients, $\Delta y = \Delta y/\Delta x = c*\Delta x$; in calculus as the derivative, $dy = (dy/dx)*dx = y'*dx$. In science as meter = (meter/second)*second = speed*second, etc. In economics as price formulas: \$ = (\$/kg)*kg = price*kg, \$ = (\$/day)*day = price*day, etc.

With physical units, recounting gives per-numbers bridging the units. Thus 4\$ per 5kg or 4/5 \$/kg gives $T = 15\text{kg} = (15/5)*5\text{kg} = (15/5)*4\$ = 3\$$; and $T = 16\$ = (16/4)*4\$ = (16/4)*5\text{kg} = 20\text{kg}$. With like units, per-numbers become fractions.

Trigonometry occurs as per-numbers when mutually recounting sides in a rectangle halved by its diagonal, $a = (a/c)*c = \sin A*c$, etc.

Modeling mixtures as 2kg at 3\$/kg + etc, unit-numbers add directly, but per-numbers P add by the area A under the per-number graph, found by slicing it thinly so that the change may be written as $dA = P*dx$ in order to use that when differences add, all middle terms disappear leaving just the endpoint difference, thus motivating developing differential calculus to find the per-number $A' = dA/dx = P$.

References

Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.

MIXING DESIGN AND DIFFERENCE RESEARCH WITH EXPERIENTIAL LEARNING CYCLES ALLOWS CREATING CLASSROOM TEACHING FOR ALL STUDENTS

Allan Tarp

MATHeCADEMY.net

International tests show that not all students benefit from mathematics education. This poor-performance-problem raises a Cinderella question: is there a hidden difference that can make the Prince dance? If so, design research can create Kolb's experiential learning cycles to adapt a given micro-curriculum so that all students may benefit.

In primary school, difference research searching for hidden differences has identified several alternatives: Digits are icons. Numbers are double-numbers with bundles as units, e.g. $T = 2\ 3s$. Flexible bundle-numbers have over- and underloads, e.g. $T = 53 = 5B3 = 4B13 = 6B-7$ tens, and ease operations as e.g. $329/7 = 32B9/7 = 28B49/7 = 4B7 = 47$, or $23*8 = 2B3*8 = 16B24 = 18B4 = 184$.

Operations are icons also where division is a broom pushing away bundles, multiplication a lift stacking bundles, subtraction a rope pulling away stacks to find unbundled, and addition the two ways to unite stacks, on-top and next-to.

Changing units may be predicted by a recount-formula $T = (T/B)*B$ coming from recounting 8 in 2s as $8 = (8/2)*2$, or, and used to solve the equation $u*2 = 8$ by recounting 8 in 2s to give the solution $u = 8/2$; thus solving most STEM-equations, typically predicting proportionality: meter = (meter/sec)*sec = speed*sec.

In middle school, double-counting leads to per-numbers becoming fractions with like units, and adding by their areas as integral calculus. In algebra, factors are units placed outside a bracket. Trigonometry occurs when mutually double-counting sides in a rectangle halved by its diagonal.

In high-school, redefining inverse operations allows equations to be solved by moving to opposite side with opposite sign. And adding per-numbers by areas allows introducing integral calculus before differential calculus.

Designing and redesigning micro-curricula as experiential learning cycles allows teachers perform design research in their own classroom, to be reported as master projects first, and later perhaps as PhD projects including more details.

References

Kolb, D. (1983). *Experiential learning*. New Jersey: Prentice Hall.

Tarp, A. (2017). *Difference-research powering PISA performance: count & multiply before you add*. Keynote presentations to the CTRAS 2017 conference in Dalian, China.

Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.

FROM PLACE VALUE TO BUNDLE-BUNDLES: UNITS, DECIMALS, FRACTIONS, NEGATIVES, PROPORTIONALITY, EQUATIONS AND CALCULUS IN GRADE ONE

Allan Tarp

MATHeCADEMY.net

Traditionally, a multi-digit number as 2345 is presented top-down as an example of a place value notation counting ones, tens, hundreds, thousands, etc.; and seldom as four numberings of unbundled, bundles, bundle-bundles, bundle-bundle-bundles, etc., to provide a bottom-up understanding abstracted from concrete examples, which would introduce exponents in primary school as the number of bundle-repetitions. Counting ten fingers in 3s thus introduces bundle-bundles: $T = \text{ten} = 3B1$ $3s = 1BB1$ $3s$.

Stacking bundles, the unbundles singles may be placed as a stack next-to leading to decimals, e.g. $T = 7 = 2.1$ $3s$; or on-top of the stack counted as bundles thus leading to fractions, $T = 7 = 2 \frac{1}{3}$ $3s$; or to negative numbers counting what is needed for another bundle, $T = 7 = 3.-2$ $3s$.

Bundles and negative numbers may also be included in the counting sequence: $0B1, 0B2, \dots, 0B7, 1B-2; 1B-1, 1B0, 1B1, \dots, 9B7, 1BB-2, 1BB-1, 1BB$.

Counting makes operations icons: division is a broom pushing away bundles, multiplication is a lift stacking bundles, subtraction is a rope pulling away stacks to find unbundled, and addition is the two ways to unite stacks, on-top and next-to.

Recounting 8 in 2s may be written as a recount-formula: $8 = (8/2)*2$, or $T = (T/B)*B$, used to solve the equation $u*2 = 8$ by recounting 8 in 2s to give the solution $u = 8/2$; thus solving most STEM-equations, typically expressing proportionality.

Once counted, stacks may add on-top after recounting changes the units to the same, or next-to by adding areas as in integral calculus. And reverse addition leads to differential calculus by pulling away the initial stack before pushing away bundles.

At the end of grade one, recounting between digits and tens leads to tables and equations when asking e.g. $T = 4$ $6s = ?$ tens, and $T = 42 = ?$ $7s$.

References

Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.

SOCIOLOGICAL IMAGINATION DESIGNS MICRO-CURRICULA FOR EXPERIENTIAL LEARNING CYCLES

Allan Tarp

MATHeCADEMY.net

Forced by peer review to focus on existing research, many education research articles fail to be validated in the classroom by observing if its educational goal is reached. However, the peer review crisis creates a need for a different research meeting its proper genre demands: reliable data and valid findings to a research question.

To help student brains adapt to the outside world, mathematics education must decide if its goal is to master inside mathematics as a means to later master outside quantity, thus risking what sociology calls a goal displacement (Bauman, 1990) where a means becomes a goal instead; or to master quantity directly if first mastering contemporary university mathematics becomes too difficult to many students.

Many curriculum reforms include competences. But again, we must ask: is the goal to obtain inside mathematical competence, or outside quantitative modeling competence?

A learning-by-doing curriculum calls for experiential learning cycles as described by Kolb's learning theory (Kolb, 1983) being adapted e.g. in the new Vietnamese curriculum; and containing cyclic phases. First micro-curriculum A is taught and validated if meeting its expected goals, next systematic observations gather reliable data as to which goals are met, and which are not, then reflections modifies the micro-curriculum into version B. Then plan B is taught, etc.

Combined with design research (Bakker, 2018), experiential learning cycles allows teachers to become action learners or action researchers in their own classroom reporting their work in master or PhD papers. To meet the genre demands of research, the data gathered must be reliable, and the findings must be tested for validity. In design research, reliability comes by making systematic observations through notes, interviews, questionnaires etc. And testing validity here means holding on to the strong parts of the actual micro-curriculum and changing the weak parts.

References

- Bakker, A. (2018). *Design research in education*. London UK: Routledge.
- Bauman, Z. (1990). *Thinking sociologically*. Oxford, UK: Blackwell.
- Kolb, D. (1983). *Experiential learning*. New Jersey: Prentice Hall.
- Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.

CONCRETE STEM SUBJECTS ALLOW MATHEMATICS LEARNING BY MODELING AND PEER-BRAIN TEACHING

Allan Tarp

MATHeCADEMY.net

Traditionally, mathematics is considered one of the core subjects in education because of the many ‘applications of mathematics’. This phrasing leads directly to the view that “of course mathematics must be learned first before it can be applied by others”. Consequently, mathematics teaches the operation order addition, subtraction, multiplication and division with cardinal numbers, later expanded to integers, rational and real numbers, again followed by expressions including also unspecified numbers.

Talking instead about outside roots leads to the opposite view that “of course, mathematics must be learned through its outside roots, also constituting its basic applications”. This ‘de-modeling’ view resonates with the fact that historically, the Pythagoreans chose the name mathematics, meaning knowledge in Greeks, as a common label for their four areas of knowledge about Many in time and pace, in time, in space and by itself: astronomy, music, geometry and arithmetic. Later the Arabs added algebra with polynomial numbers created by systematic bundling. Here the outside roots are evident through the original meanings of geometry and algebra: earth-measuring and reuniting.

So, mathematics grew and may still grow from counting, recounting and double-counting bundles, and from applying science, describing forces pumping motion in and out of matter when having the same or opposite directions.

Working in groups with science applications allows students to learn through peer-brain teaching instead of through wiser-brain teaching. As to matter, tasks could be to find its mass, its center, its density, and the heat transfer under collision between visible macro-matter and invisible micro-matter, applied in steam power, or when placing ice-cubes in water.

As to motion, tasks could be to describe traveling with constant or changing speed horizontally or on an incline, vertical motion, projectile orbits; and circular motion, swings or see-saws on a market place. As well as how to use electrons to store or transport motion and information.

References

- Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.
- Tarp, A. (2018). *Addition-free STEM-based Math for Migrants*. Paper presented at the CTRAS 2019 conference at Beijing Normal University June 28-30 2019.
- Tarp, A. (2019). *De-modeling numbers, operations and equations: from inside-inside to outside-inside understanding*. Proceedings from Psychology and Mathematics education conference at the Ho Chi Minh City University of Education on December 7, 2019.

THE SIMPLICITY OF MATHEMATICS DESIGNING A STEM-BASED CORE CURRICULUM FOR REFUGEE CAMPS

Allan Tarp

MATHeCADEMY.net

A number as 2345 may evade the place value notation if seen as four numberings of unbundled, bundles, bundle-bundles, bundle-bundle-bundles. Here exponents occur as the number of bundling-repetitions, e.g. when counting ten fingers as $T = \text{ten} = 3B1\ 3s = 1BB1\ 3s$.

Stacking bundles in blocks, the unbundled singles may be placed as a stack next-to leading to decimals, e.g. $T = 7 = 2.1\ 3s$; or on-top of the stack counted as bundles leading to fractions, $T = 7 = 2\ 1/3\ 3s$, or to negative numbers counting what is needed for another bundle, $T = 7 = 3.-2\ 3s$.

Bundles and negative numbers may also be included in the counting sequence: $0B1, 0B2, \dots, 0B7, 1B-2; 1B-1, 1B0, 1B1, \dots, 9B7, 1BB-2, 1BB-1, 1BB$.

Counting makes operations icons: division is a broom pushing away bundles, multiplication is a lift stacking bundles, subtraction is a rope pulling away stacks to find unbundled, and addition is the two ways to unite stacks, on-top and next-to.

Recounting 8 in 2s may be written as a recount-formula: $8 = (8/2)*2$, or $T = (T/B)*B$, used to solve the equation $u*2 = 8$ by recounting 8 in 2s to give the solution $u = 8/2$; thus solving most STEM-equations, typically expressing proportionality.

Once counted, stacks may add on-top after recounting changes the units to the same, or next-to by adding areas as in integral calculus. And reverse addition leads to differential calculus by pulling away the initial stack before pushing away bundles.

Recounting between digits and tens leads to tables and equations when asking e.g. $T = 4\ 6s = ?\ \text{tens}$, and $T = 42 = ?\ 7s$. Recounting in different units gives per-numbers bridging the units, becoming fractions with like units, and adding by areas. Mutually recounting sides in a block halved by its diagonal gives trigonometry.

References

Tarp, A. (2018). Mastering Many by counting, re-counting and double-counting before adding on-top and next-to. *Journal of Mathematics Education*, 11(1), 103-117.